

**Ph.D. thesis:**

***Comparison of Parsimonious  
Dynamic Vegetation Modelling  
Approaches in Semiarid Climates***

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**Ph.D. Program in Hydraulic  
and Environmental  
Engineering**



**Instituto de Ingeniería del  
Agua y Medio Ambiente**



**UNIVERSITAT  
POLITÈCNICA  
DE VALÈNCIA**



**Grupo de Investigación de Modelación Hidrológica y Ambiental**

- Introduction
- Remote Sensing of Vegetation
- Study Case
- Vegetation Models
- Results and Discussion
- Conclusions



Arid and semi arid climate



tight interconnection  
between vegetation and  
hydrological processes

COUPLED MODELLING  
hydrology - vegetation

focus on  
PARSIMONIOUS  
MODELS

LOW availability of  
FIELD DATA

use REMOTE  
SENSING data

not direct observations of  
vegetation characteristics

need for INTERPRETATION

VEGETATION  
MODELLING

SATELLITE  
INFORMATION

Leaf Area Index (**LAI**)  
leaf area / ground area

- very important vegetation variable
- field measurements are complex

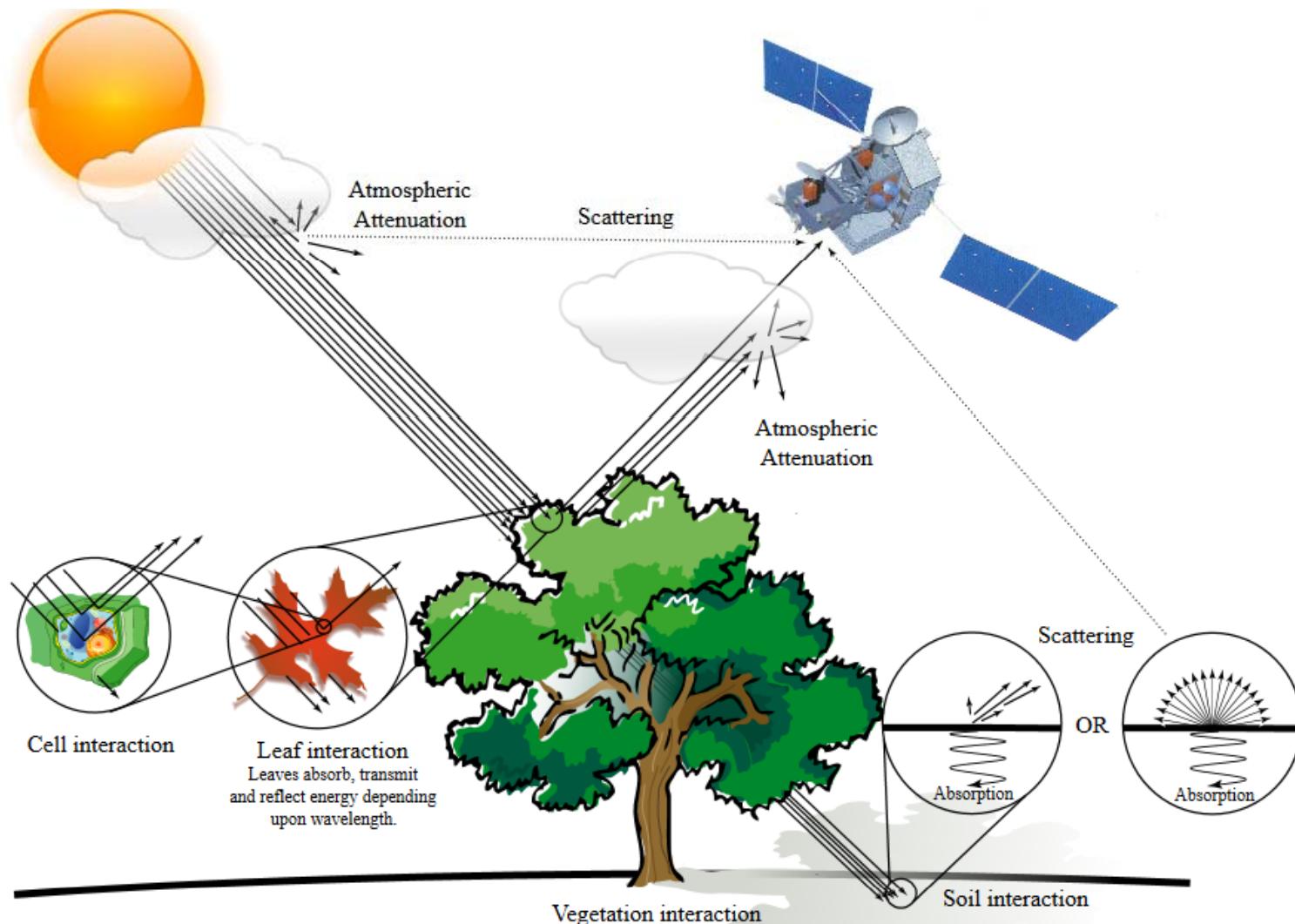
# Research questions

- which parsimonious **vegetation model** is most suitable to reproduce vegetation dynamics in semi arid environments?  
(need for reliable models!)
- which remote sensing **vegetation indices** provide information suitable to assess models' performance?  
(indirect observations)

- identification of a **study area**: Aleppo pine forest in Valdeinfierno catchment (SE Spain)
- identification of suitable parsimonious **vegetation models** (for semi arid environments)
- analysis of vegetation-related **satellite data**
- **modelling** of vegetation dynamics
- analysis of **results and conclusions**

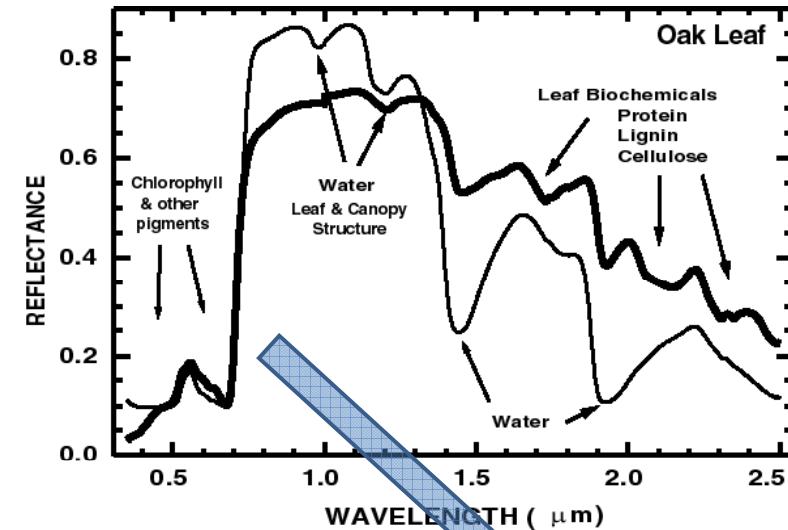
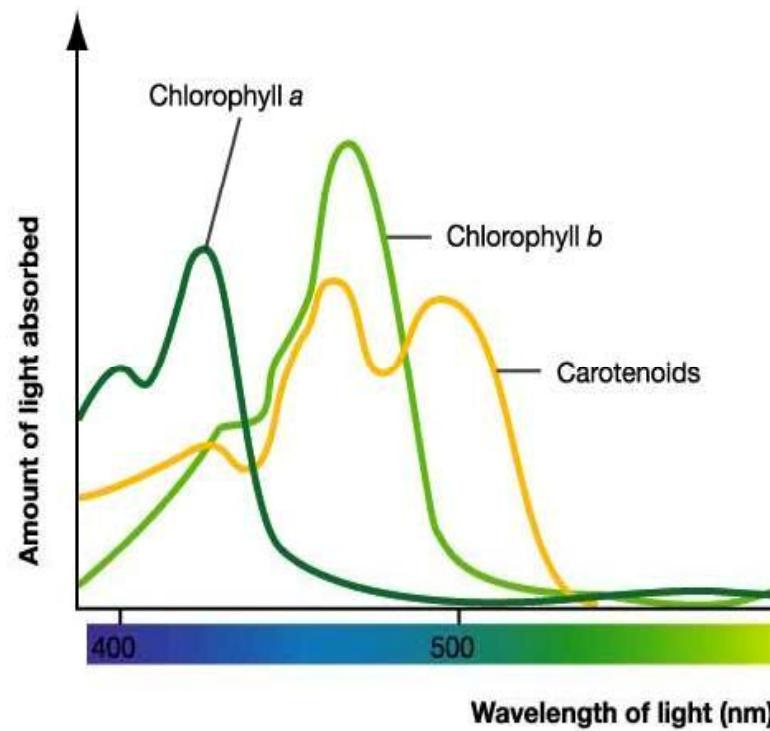


# Remote sensing of vegetation





# Remote sensing of vegetation



Reflection  
in the near  
infra-red

Absorption  
in the red

# Vegetation Indices

**GNDVI**

**NDWI**

**GARI**

**SR**

**NDVI**

**MSAVI**

**SAVI**

**GVMI**

**PVI**

**EVI**

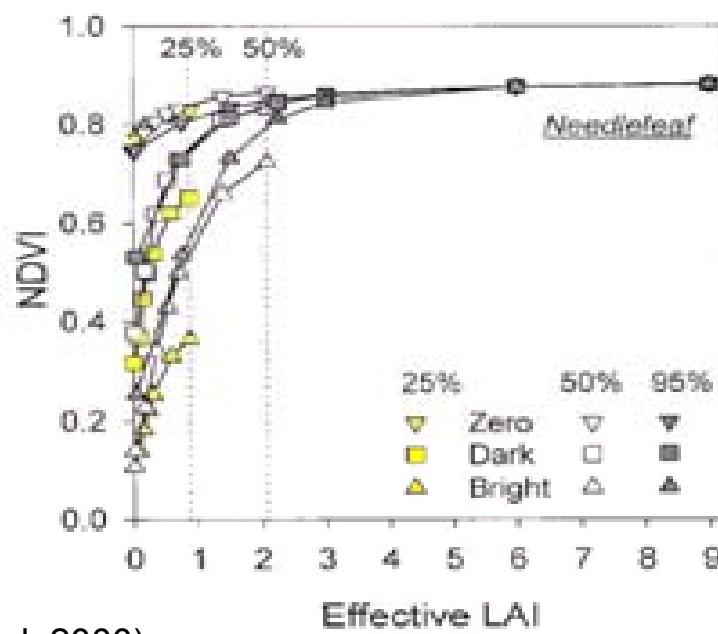
**TSAVI**



Grupo de Investigación de Modelación Hidrológica y Ambiental

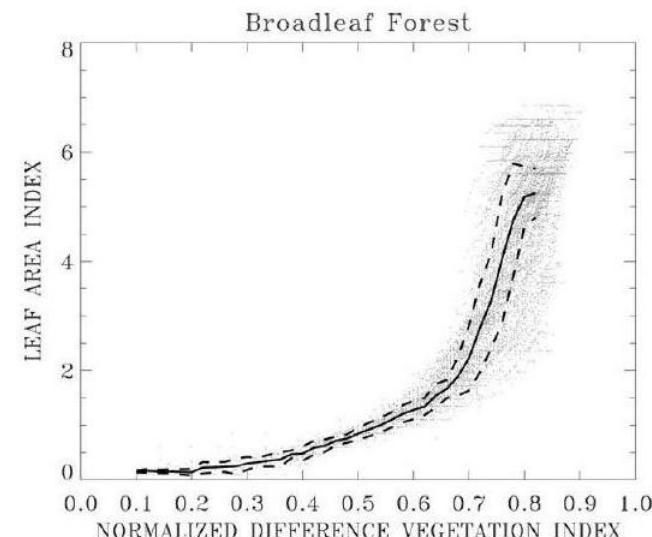
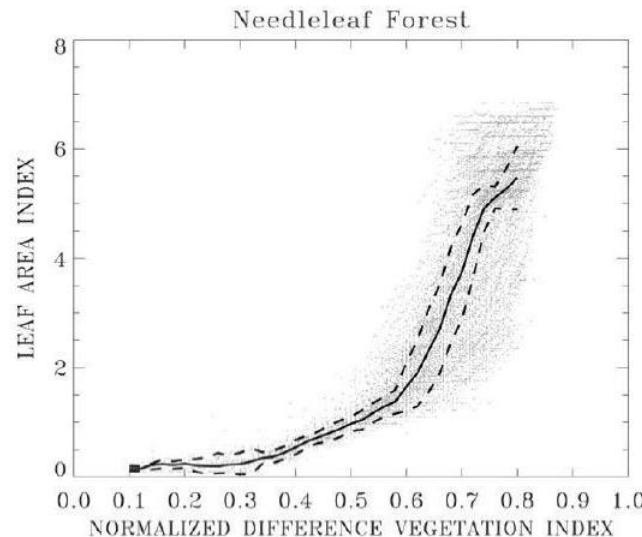
$$NDVI = \frac{NIR - red}{NIR + red}$$

(Rouse et al, 1973)



(Gao et al, 2000)

- Sensitive to green biomass
- Useful to monitor photosynthetically active biomass
- Influenced by background brightness
- NDVI vs. LAI: non-linear and saturation for dense canopies



(Buermann et al, 2002)

$$LAI_{NDVI} = -\frac{1}{k} \ln \frac{NDVI_{can} - NDVI}{NDVI_{can} - NDVI_{back}}$$

(Gigante et al, 2009)

$NDVI_{can}$ : value to which NDVI tends at high vegetation density

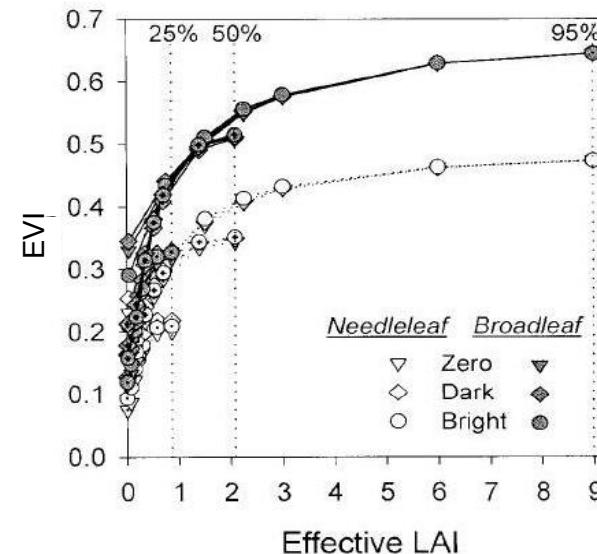
$NDVI_{back}$ : NDVI value corresponding to very low vegetated soil

k: extinction coefficient

$$EVI = G \cdot \frac{(NIR - red)}{(NIR + C1 \cdot red - C2 \cdot blue + L)}$$

(Huete et al, 2002)

- Enhancement of vegetation signal:
  - correction for soil background
  - reduction in atmospheric influence
- Highly responsive to LAI



(Gao et al, 2000)

## MODERATE-RESOLUTION IMAGING SPECTRORADIOMETER

- onboard Terra and Aqua satellites
- data every 1 - 2 days
- 36 spectral bands
- spectral range 0.4 - 14.4  $\mu\text{m}$
- spatial resolution depending on the bands (250, 500, 1000 m)



Good resolution in time and space for this research objectives.

# Other MODIS products

## LEAF AREA INDEX

(Mynden et al, 2003)

Algorithm needing:

- spectral information
- land cover classification

Observed vs. modelled  
BRDFs for different canopy  
structures and soil patterns.

If modelled and observed  
BRDFs  $\approx$ , correspondent  
LAI is accepted.

BRDFs: Bidirectional Reflectance Distribution Functions



## ACTUAL EVAPOTRANSPIRATION

(Mu et al, 2011)

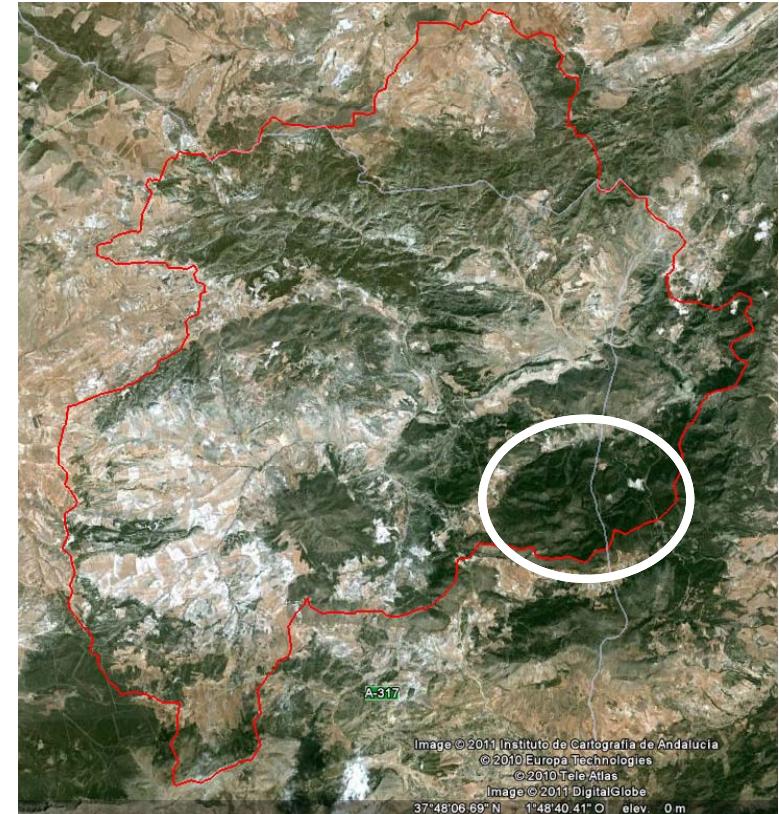
Algorithm needing:

- remote sensing inputs  
(land cover, LAI, albedo, FPAR)
- meteorological inputs  
(air pressure, air temperature,  
humidity, radiation)

# Study site - characteristics



SE of Spain – Province of Almeria

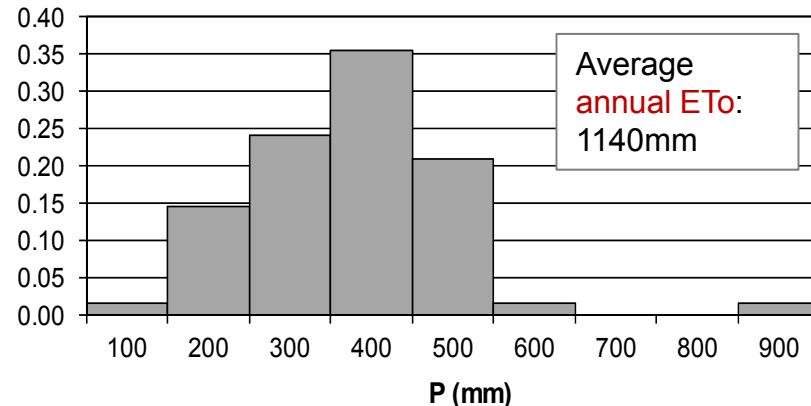


20 km<sup>2</sup> Aleppo pine forest

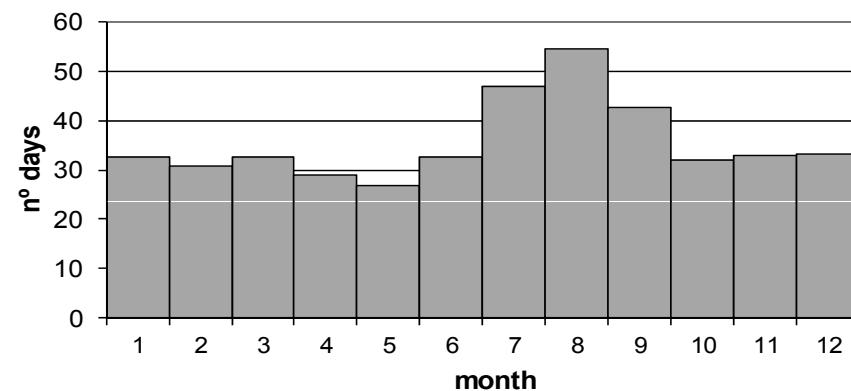


# Study site – climate

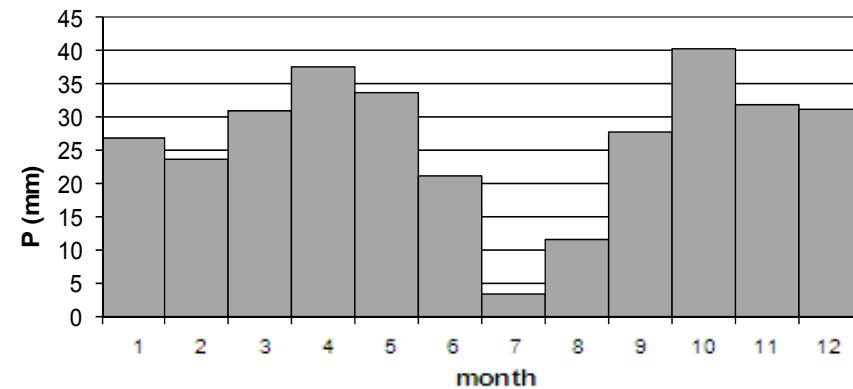
Relative frequency of annual precipitation. Average: 327 mm



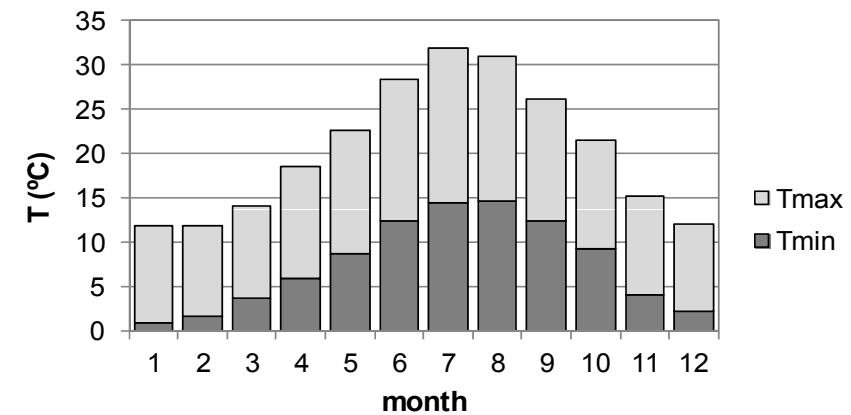
Average nº of consecutive dry days

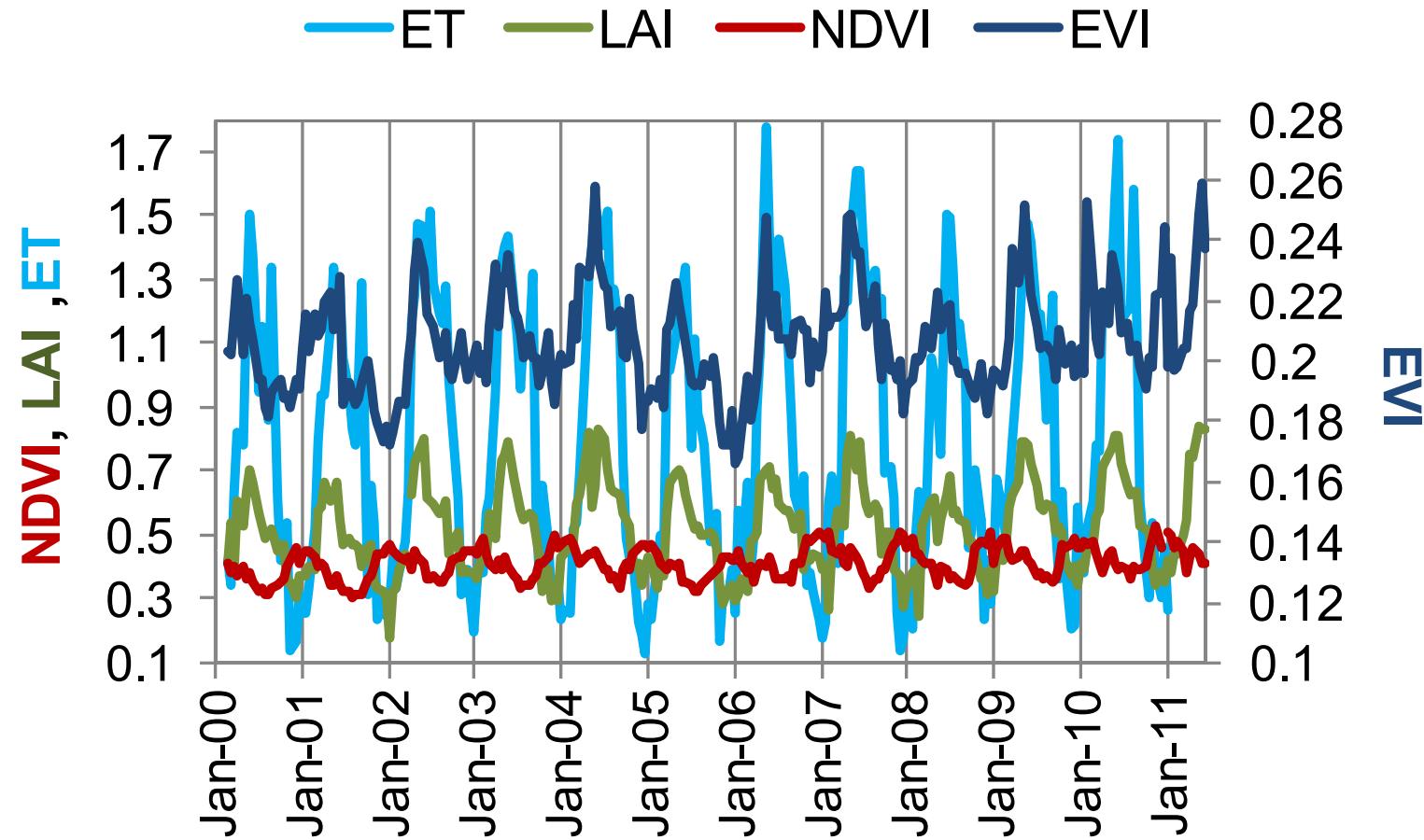


Mean monthly precipitation



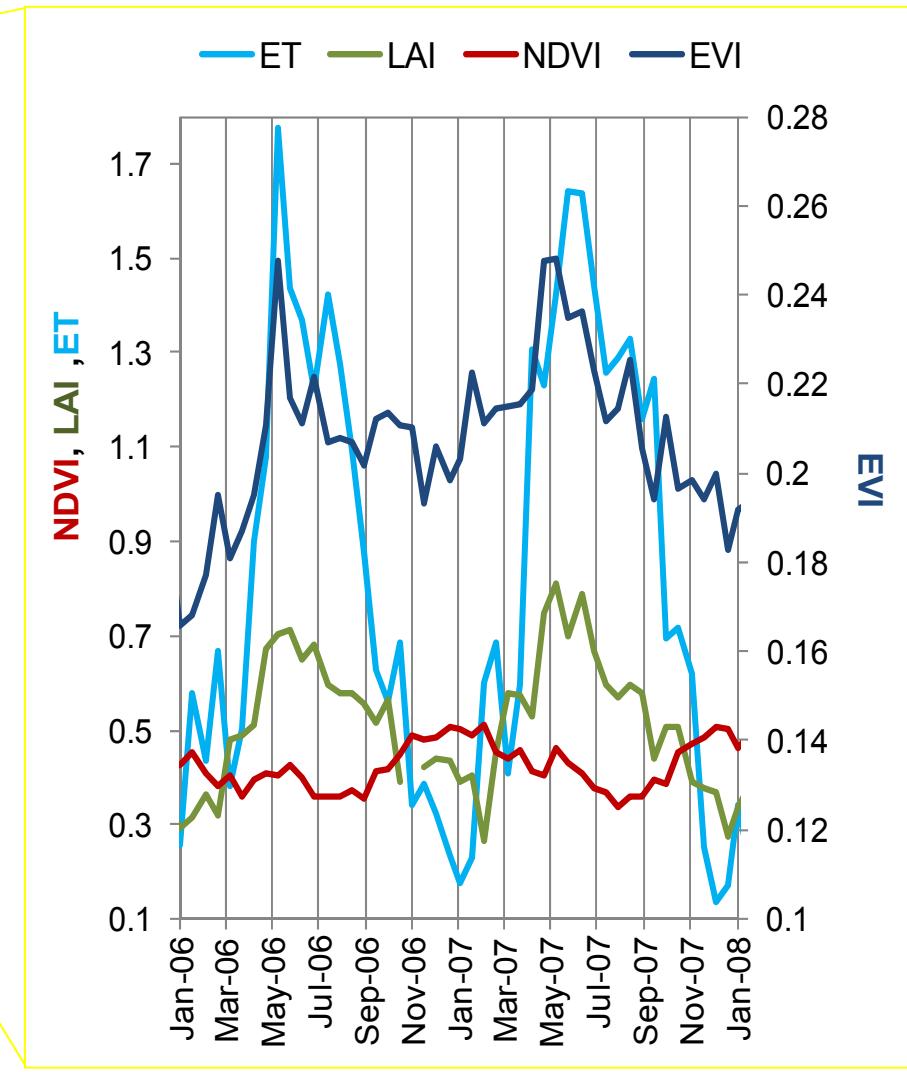
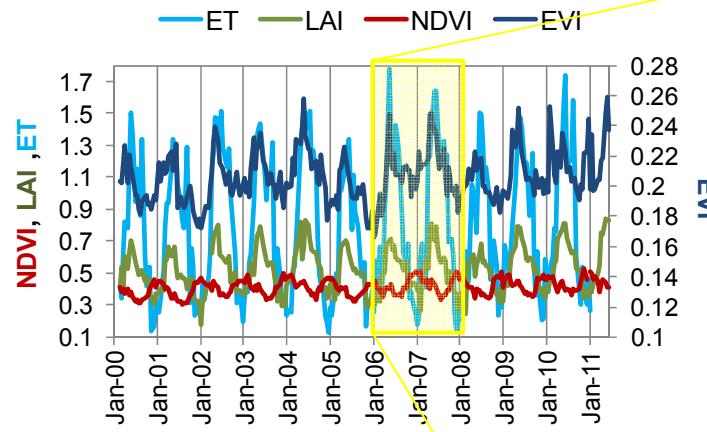
Max and min temperatures

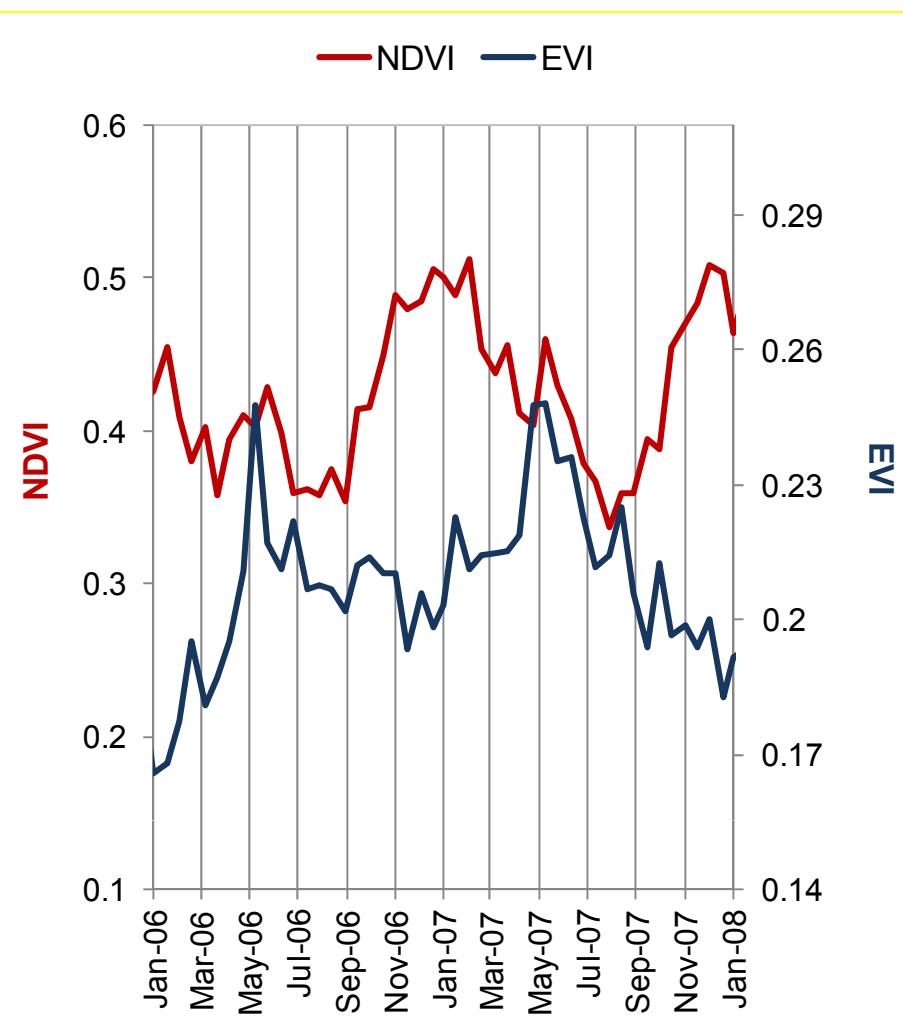
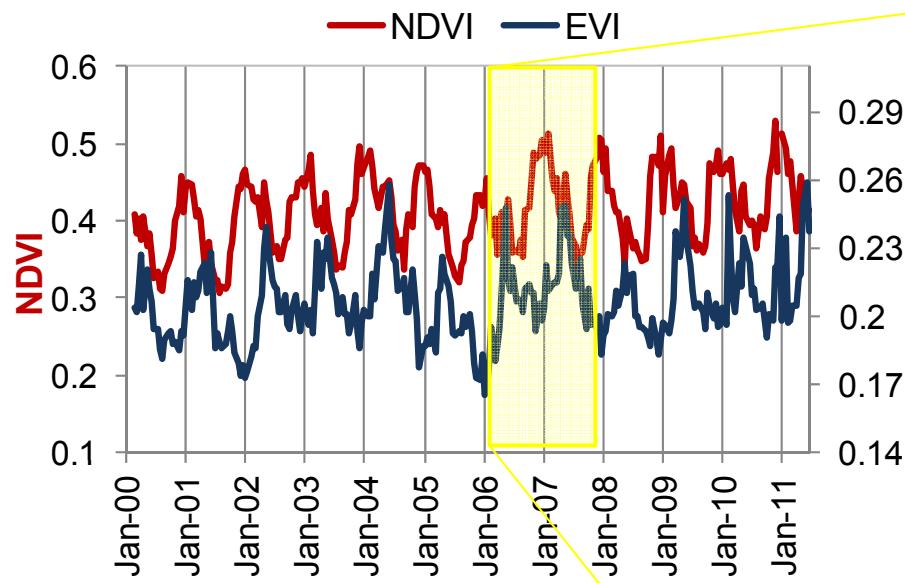






# Satellite data



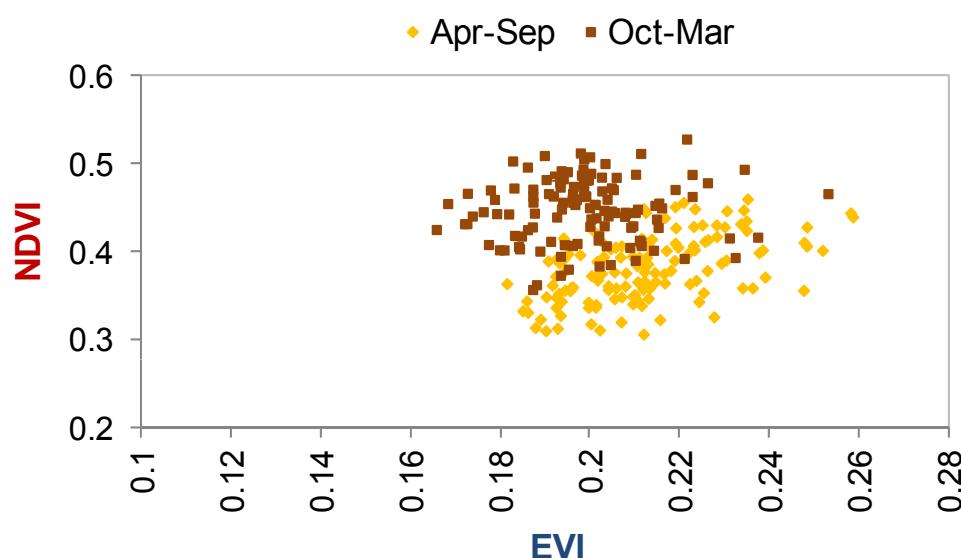


# NDVI vs. EVI

t-distribution test (95% confidence level)



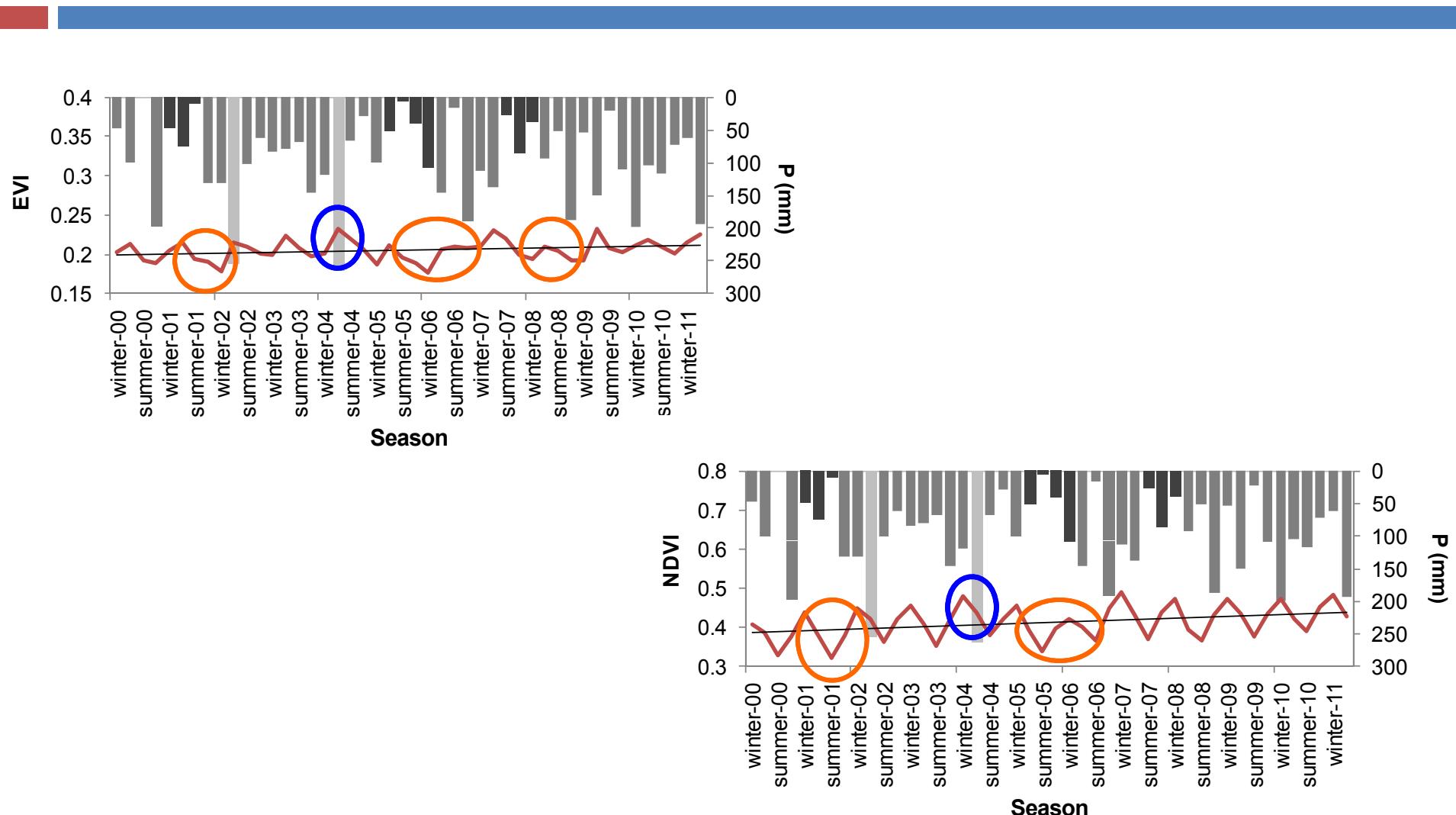
NO correlation  
but  
data April – September:  $r = 0.66$



EVI  
↔  
Aleppo p. phenology  
(Calatayud et al, 2000; Pardos et al, 2003)

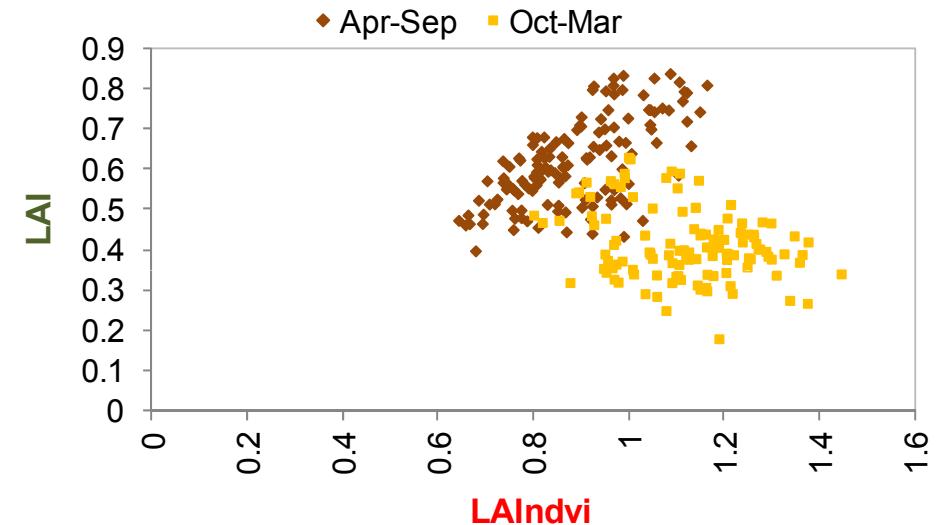
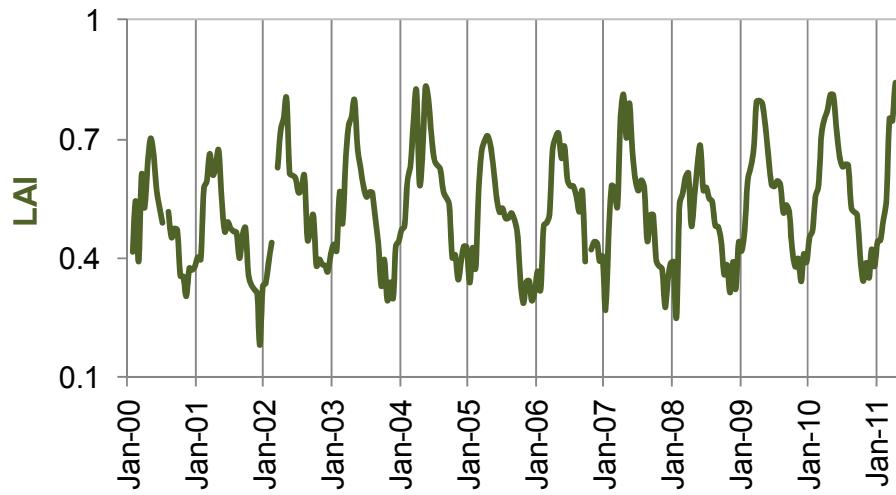
NDVI  
↔  
water stress  
changes in chlorophyll content  
(Baquedano, 2006)





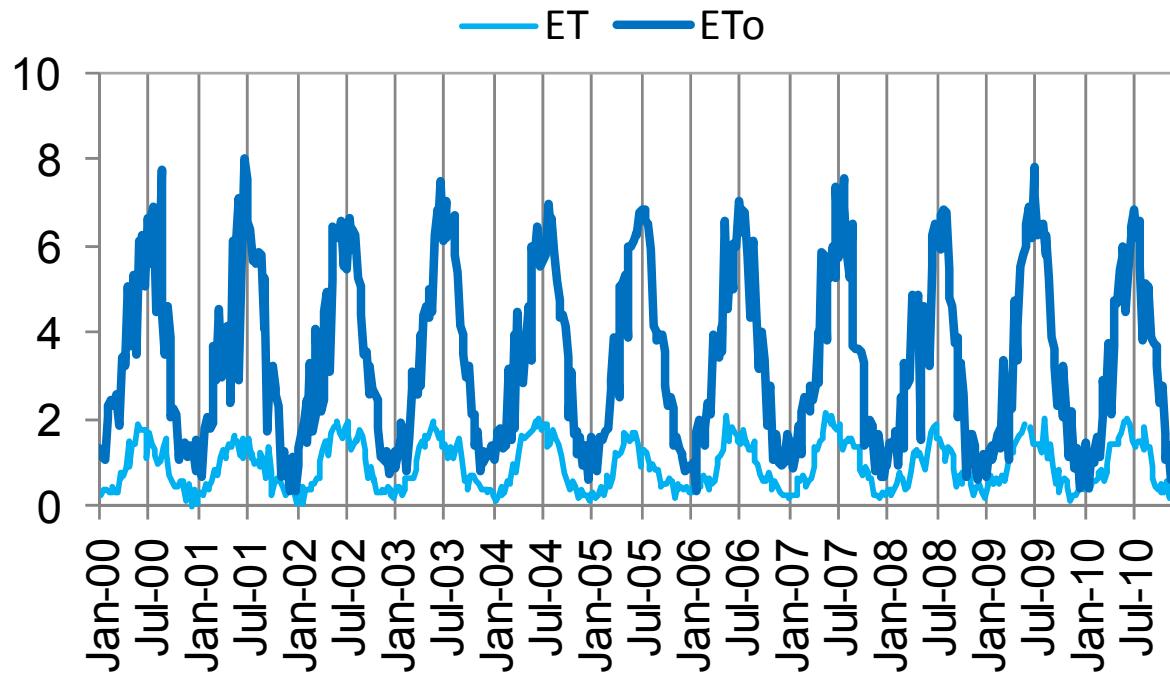


## LAI vs. LAI<sub>NDVI</sub>



WRONG land cover  
classification

...DOUBTS...field campaign (August '12) → values 1 - 2  
0.5 corresponds to just 16% forest cover (Molina & Del Campo, 2012)



HIGH CORRELATION ( $r = 0.79$ )

Obtained from  
satellite LAI

## Which characteristics do we seek?

- focused on semiarid environments
- requiring information commonly available
- simple models

# Simple vs. complex models

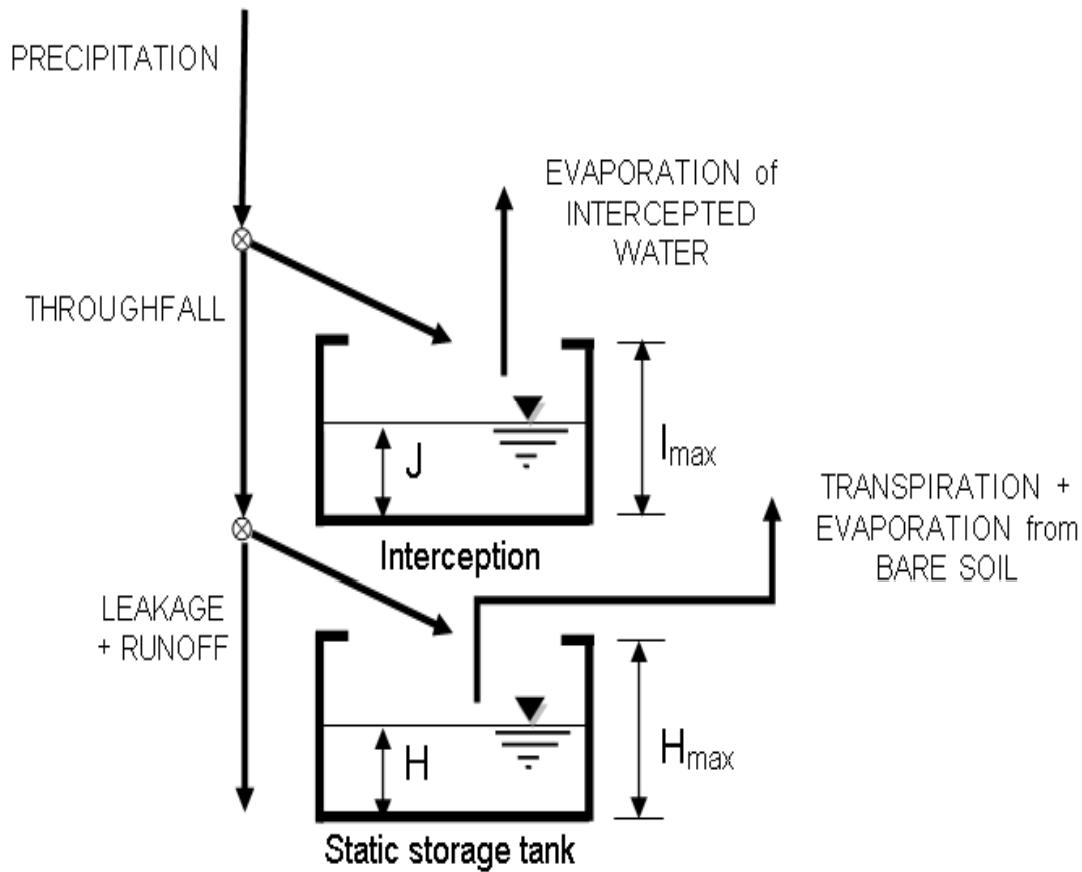
## COMPLEX MODELS:

- accurate description of the processes
- high n° of parameters (and data required)
- computational burden
- sensation of total reliability

## SIMPLE MODELS:

- processes are schematised
- low n° of parameters
- the most important processes need to be correctly reproduced

It depends on the  
OBJECTIVES  
of the research



WATER BALANCE EQ.

$$\frac{dH}{dt} = (P - I) - L - E - T$$

INTERCEPTION

$$I = P \cdot R$$

INTERCEPTION STORAGE

$$\frac{dJ}{dt} = I - \min(ET_o \cdot R, J)$$

$$\frac{dR}{dt} = \frac{A_{n,mx}}{B_{pot}} \left( \frac{T}{T_{mx}} \right)^c - k_{ws} \cdot R \cdot \zeta$$

(Quevedo and Francés, 2008)

**State variable:** R (relative leaf biomass)

**5 parameters:**  $A_{n,mx}$  (maximum net carbon assimilation)

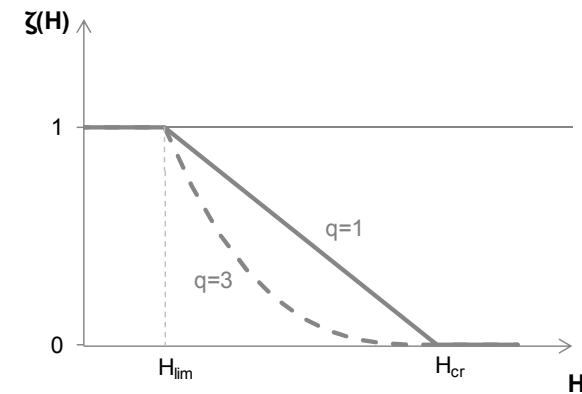
$B_{pot}$  (potential foliar biomass)

$T_{mx}$  (maximum transpiration)

c (shape exponent)

$k_{ws}$  (water stress leaf shedding coefficient )

$$\zeta(H) = \begin{cases} 0 & \text{for } H \geq H_{cr} \\ \left( \frac{H_{cr} - H}{H_{cr} - H_{lim}} \right)^q & \text{for } H_{lim} < H < H_{cr} \\ 1 & \text{for } H \leq H_{lim} \end{cases}$$



$$T = ET_o \cdot R \cdot \beta_t$$

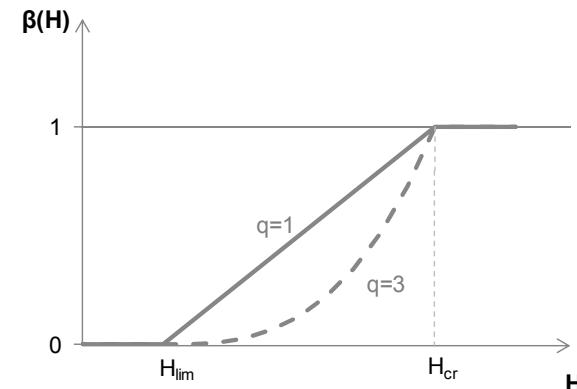
$$T = ET_o \cdot \lambda_v \cdot \lambda_s$$

$$\beta(H) = \begin{cases} 1 & \text{for } H \geq H_{cr} \\ \left( \frac{H - H_{lim}}{H_{cr} - H_{lim}} \right)^q & \text{for } H_{lim} < H < H_{cr} \\ 0 & \text{for } H \leq H_{lim} \end{cases}$$

$$E = H \cdot \left( \frac{z_{ss}}{z_e} \right) \cdot (1 - R)$$

TRANSPIRATION

FAO EQUATION  
(Allen et al, 1998)



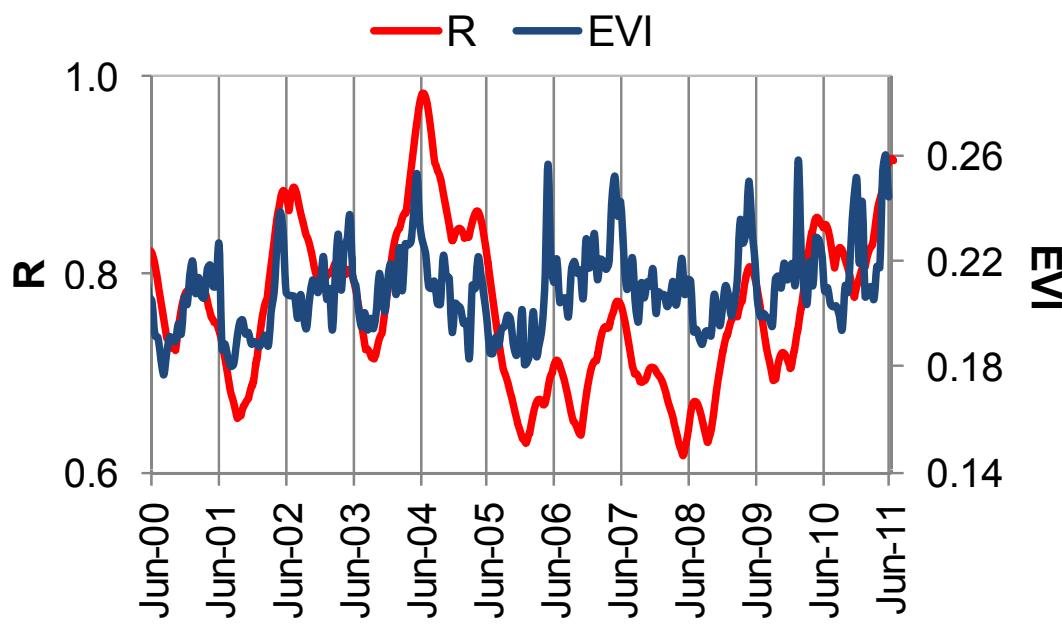
BARE SOIL  
EVAPORATION

# Modelling - HORAS

## CALIBRATION

max Pearson correlation coefficient ( $r$ ) between R and EVI

Parameters	Description	Calibrated value
$\alpha$	Ratio between maximum net carbon assimilation and potential foliar biomass [ $d^{-1}$ ]	0.0018
$T_{mx}$	Maximum transpiration ratio [ $mm\ d^{-1}$ ]	5.5
$c$	Shape exponent	0.054
$k_{ws}$	Water stress-dependent leaf shedding coefficient	0.0035



## FINAL RESULT

$$r = 0.39$$

## PROBLEMS

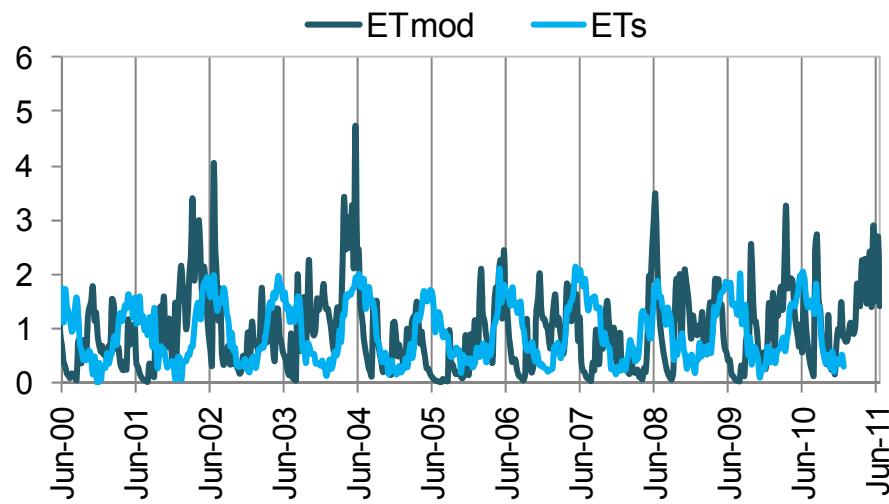
Annual cycle not clear  
(2002-2003; 2004-2005)

Marked drop (2005)



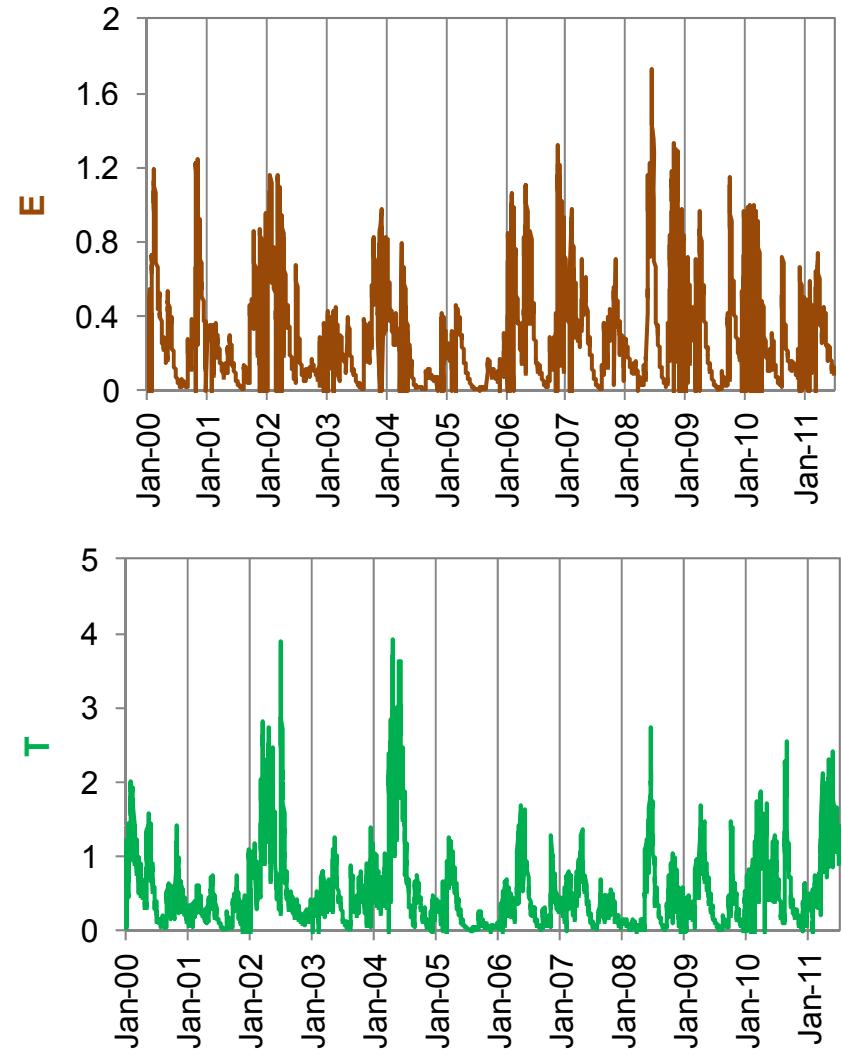
# Modelling - HORAS

$ET_{mod}$  → prolonged periods value  $\approx 0$



$E$  → average:  $0.3 \text{ mm d}^{-1}$   
max:  $1.7 \text{ mm d}^{-1}$

$T$  → average  $0.5 \text{ mm d}^{-1}$   
max:  $3.9 \text{ mm d}^{-1}$



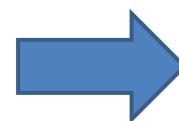
# Modelling - HORAS

**E** → 31% of ET  
vs.  
23% simulated  
bare soil

**T** → 56% of ET  
vs.  
77% simulated  
veg. cover

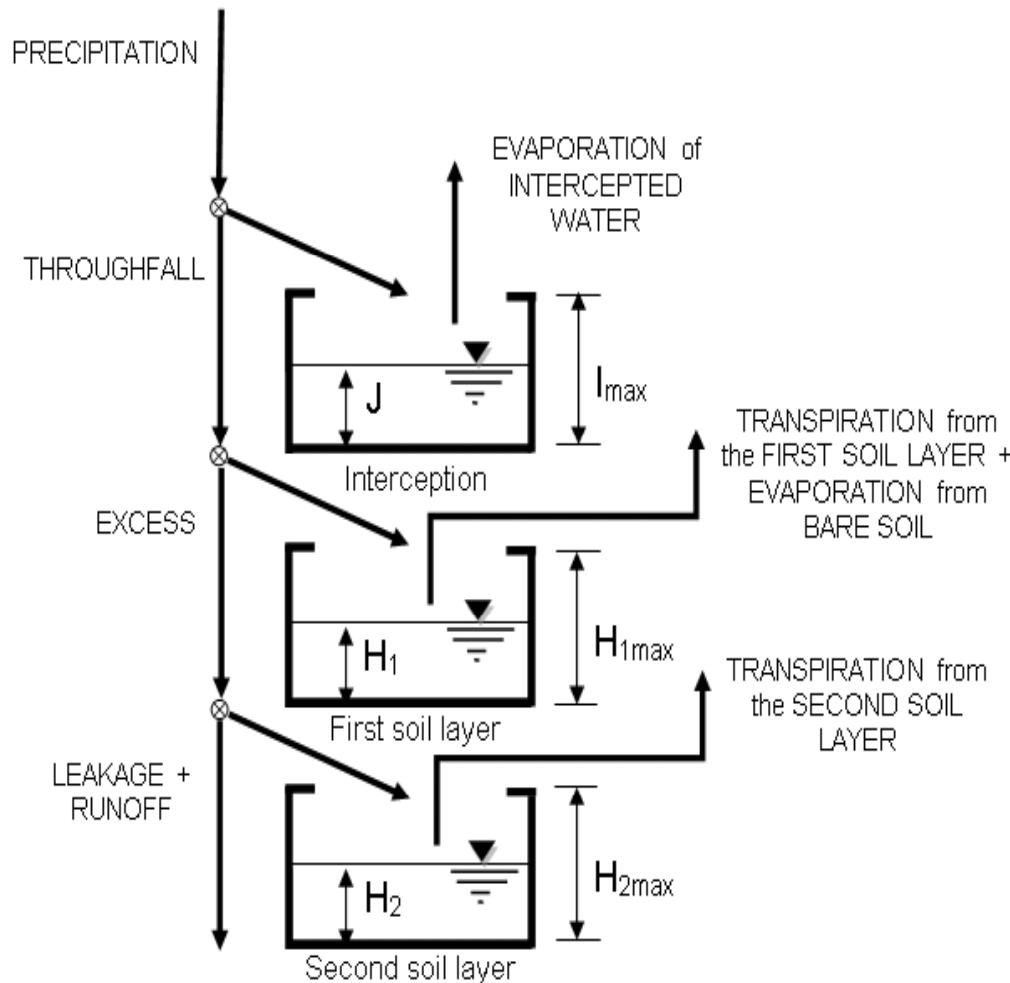
WHY?

Not correct to assume  
superficial soil layer ( $\rightarrow E$ ) with  
same moisture content of the  
entire root soil depth



For WUE- and LUE-  
models: 2 soil layers  
(1°  $\rightarrow E+T$ ; 2°  $\rightarrow T$ )

# WUE and LUE models



**WATER BALANCE EQ.**

$$\frac{dH_1}{dt} = (P - I) - D - E - T_1$$

$$\frac{dH_2}{dt} = D - L - T_2$$

**INTERCEPTION**

$$I = P \cdot f_t$$

**INTERCEPTION STORAGE**

$$\frac{dJ}{dt} = I - \min(ET_o \cdot f_t, J)$$

# WUE and LUE models

$$\frac{dB_l}{dt} = (T \cdot WUE \cdot \rho_v \cdot \omega - Re) \cdot \varphi_l - k_l \cdot B_l$$

**WATER USE EFFICIENCY**

**WUE** → [kg DM kg<sup>-1</sup> H<sub>2</sub>O]

(Williams and Albertson, 2005)

$$\frac{dB_l}{dt} = (APAR \cdot LUE \cdot \varepsilon - Re) \cdot \varphi_l - k_l \cdot B_l$$

**LIGHT USE EFFICIENCY**

**LUE** → [kg DM m<sup>-2</sup> MJ<sup>-1</sup>]

(Monteith, 1972)

**State variable:**  $B_l$  - leaf biomass  
[kg DM m<sup>-2</sup> veg cover]

**4 parameters:** **WUE** – water use efficiency  
**ω** – conversion CO<sub>2</sub> → DM  
**φ<sub>l</sub>** – allocation term  
**k<sub>l</sub>** – turnover coefficient

**LUE** – light use efficiency  
**ε** – stress coefficient  
**φ<sub>l</sub>** – allocation term  
**k<sub>l</sub>** – turnover coefficient

# WUE and LUE models

$$T_1 = ET_o \cdot f_t \cdot \min(LAI_{mod}, 1) \cdot \beta_t(H_1) \cdot r_1$$

$$T_2 = ET_o \cdot f_t \cdot \min(LAI_{mod}, 1) \cdot \beta_t(H_2) \cdot (1 - r_1)$$

**TRANSPIRATION**  
(Williams and Albertson,  
2005)

$$T = ET_o \cdot \lambda_v \cdot \lambda_s$$

**FAO EQUATION**  
(Allen et al, 1998)

$$E = ET_o \cdot f_b \cdot \beta_b(H_1)$$

**BARE SOIL  
EVAPORATION**

# WUE and LUE models

$$\varphi = 1 - \frac{LAI}{LAI_{\max}}$$

**ALLOCATION FACTOR**  
(Williams and Albertson, 2005)

$$LAI_{\text{mod}} = B_l \cdot SLA \cdot f_t$$

**GROUND BASED LAI**  
(Williams and Albertson, 2005)

$$LAI^{*}_{\text{mod}} = LAI_{\text{mod}} \cdot \left(1 - \zeta_{10}\right)$$

**CORRECTED LAI**  
(Williams and Albertson, 2005)

$$\zeta(H) = \begin{cases} 0 & \text{for } H \geq H_{cr} \\ \left(\frac{H_{cr} - H}{H_{cr} - H_{\lim}}\right)^3 & \text{for } H_{\lim} < H < H_{cr} \\ 1 & \text{for } H \leq H_{\lim} \end{cases}$$

**WATER STRESS**  
(Porporato et al, 2001)

$$\zeta_{tot} = \zeta(H_1) \cdot r_1 + \zeta(H_2) \cdot (1 - r_1)$$

**TOTAL WATER STRESS**  
(Williams and Albertson, 2005)

# Sensitivity analysis

Which parameters mostly affect models' performance?



GSA (general sensitivity analysis)  
8 parameters  
(Hornberger and Spear, 1980)



3958 behaviours and 56042 non-behaviours for the WUE-model

16893 behaviours and 43107 non-behaviours for the LUE-model.

**WUE- model  
LUE-model**

Montecarlo technique:

60,000 independent sets of parameters (random from uniform distributions)

Objective function: RMSE  
( $\text{LAI}_{\text{NDVI}}$  vs.  $\text{LAI}^{\text{mod}}$ )

Threshold RMSE = 0.2

Sets of parameters divided into behavioural / non-behavioural ones

## Kolmogorov-Smirnov two-sample test

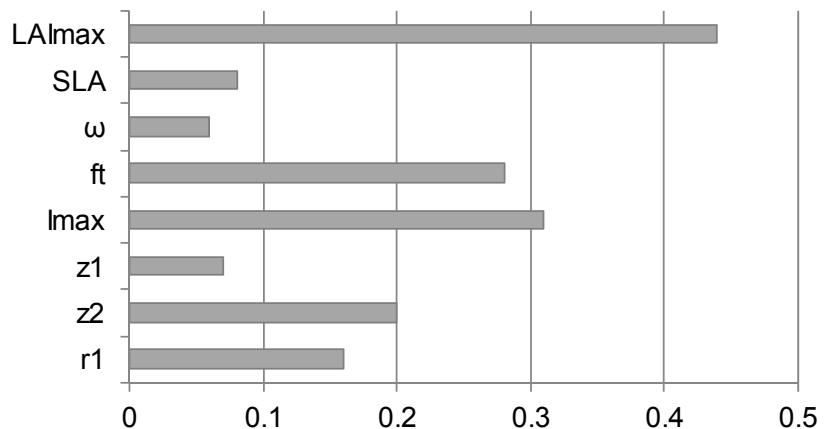
(Kolmogorov, 1933; Smirnov, 1948)

Cumulative probability distribution curves for the behaviours and non-behaviours

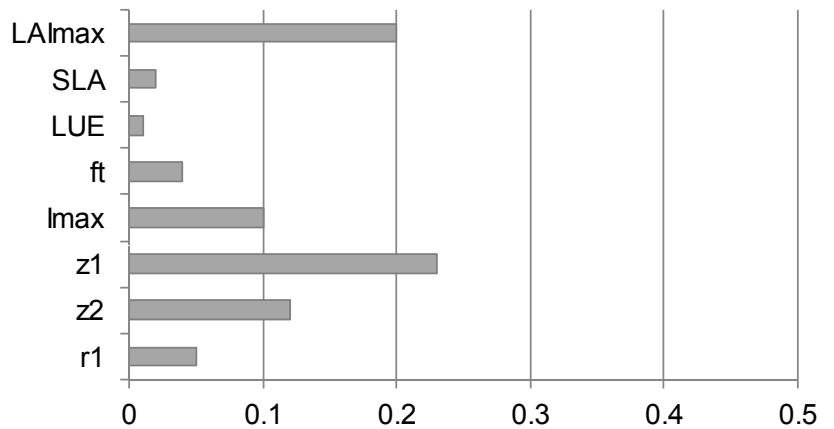
Measure of the maximum vertical distance between the curves (KS)

The larger the value of the KS index, the higher the importance of the considered parameter in determining the simulation result.

WUE-model



LUE-model



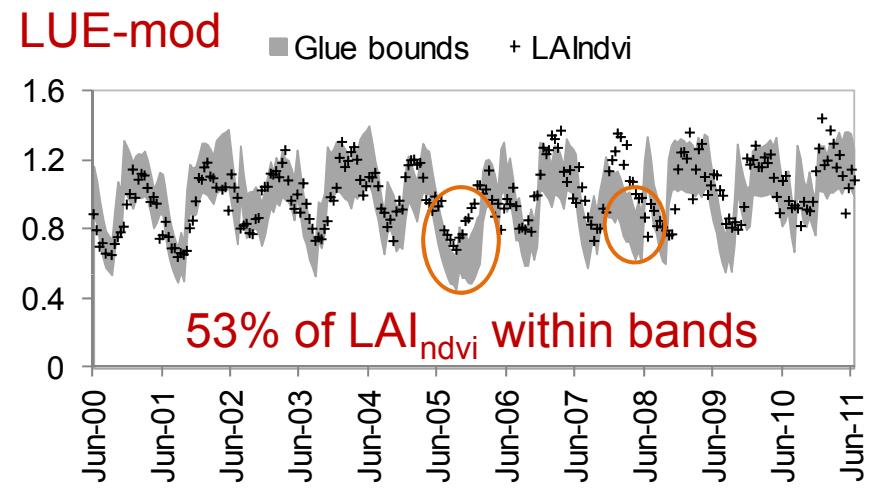
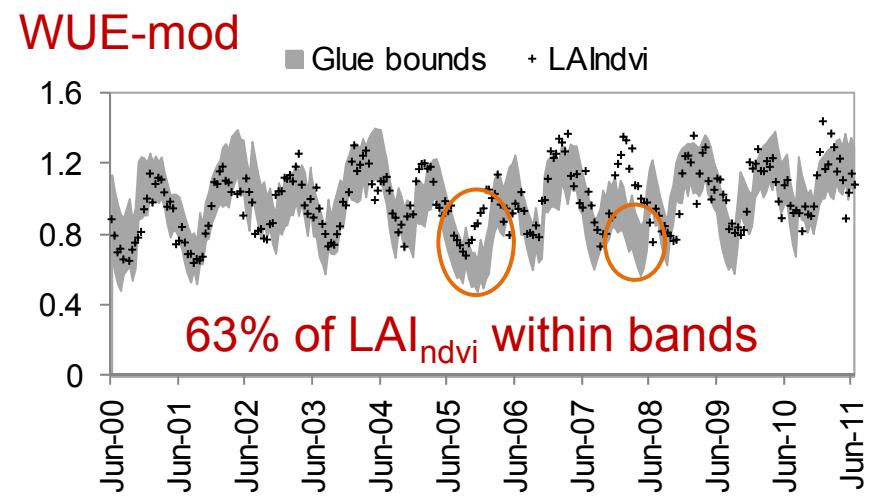
## GLUE: General Likelihood Uncertainty Estimation

(Beven and Binley, 1992)

To test the models' capability in reproducing vegetation dynamics, and their robustness

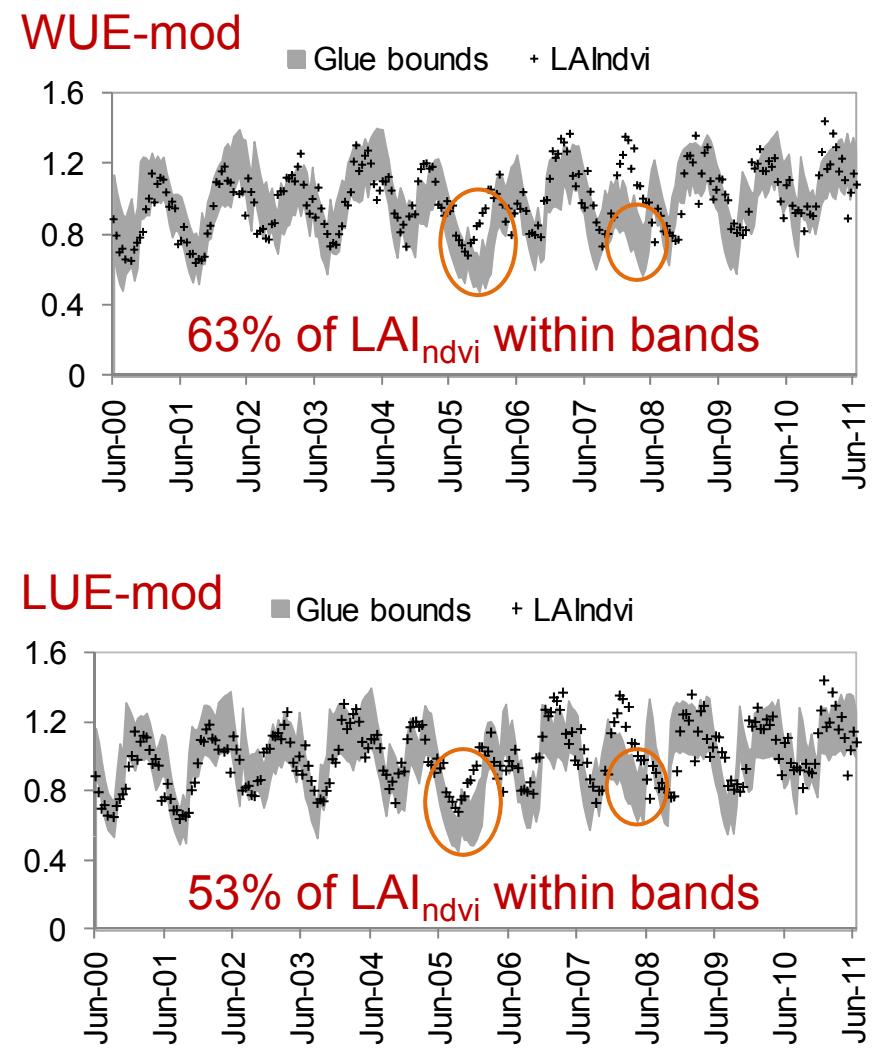
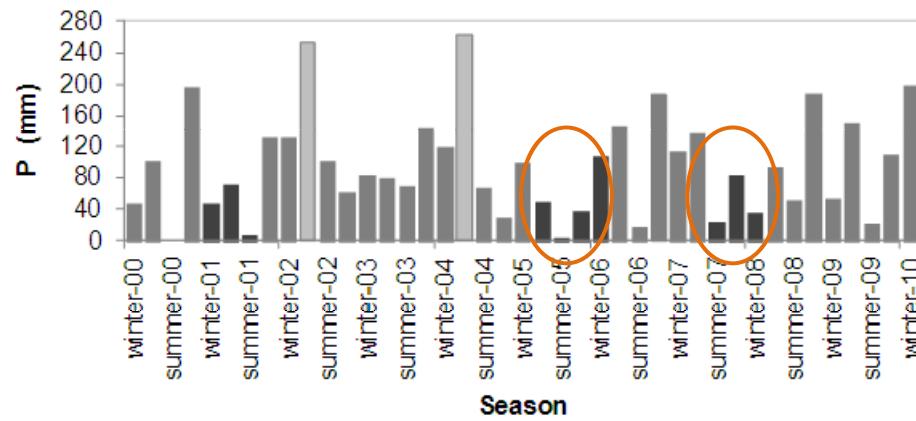
Calculating the likelihood-weighted distribution of the outputs corresponding to the accepted sets of parameters

Computing the 90% GLUE band (5% and 95% percentiles as bounds)



## GLUE: General Likelihood Uncertainty Estimation

(Beven and Binley, 1992)



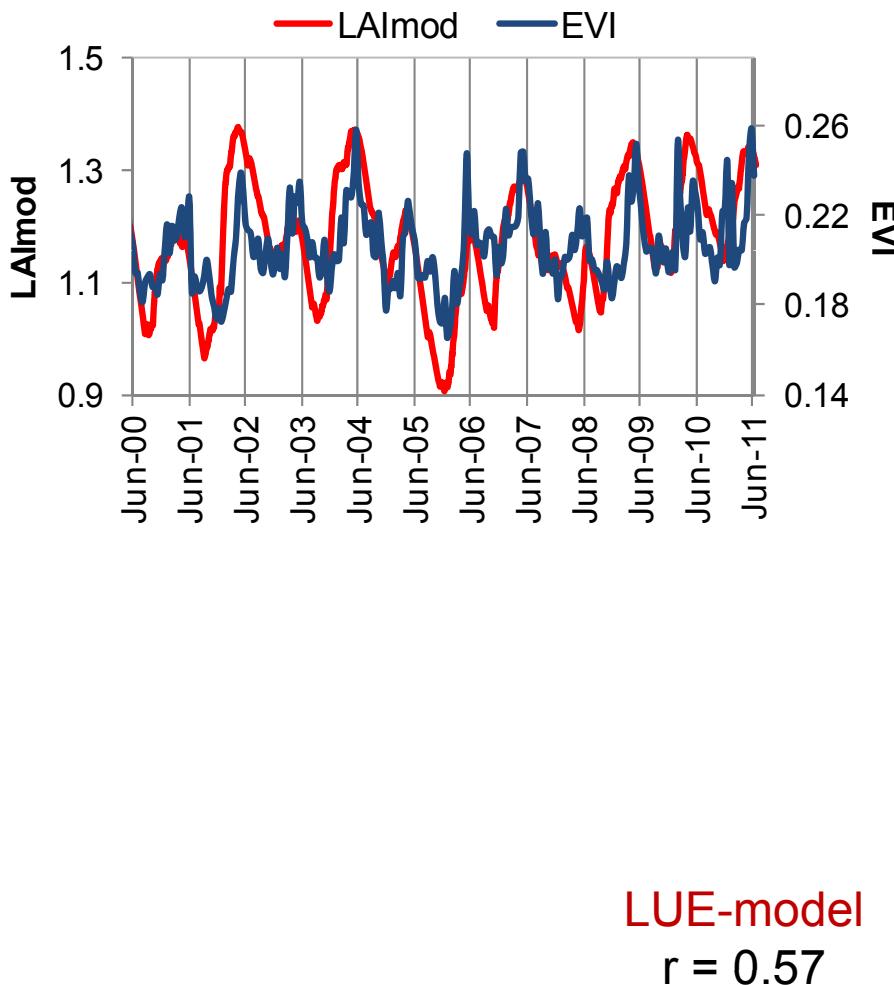
Genetic algorithm



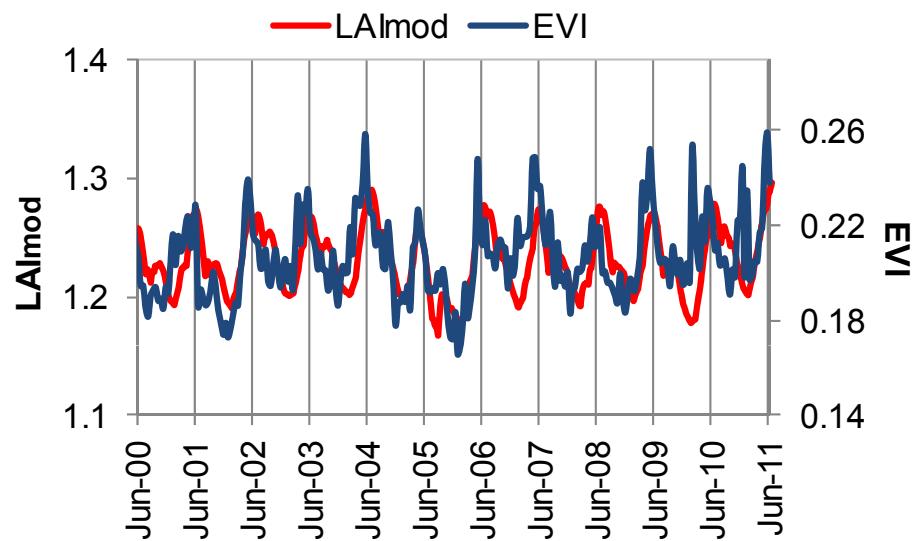
minimize RMSE  
( $\text{LAI}_{\text{mod}}^*$  vs.  $\text{LAI}_{\text{NDVI}}$ )

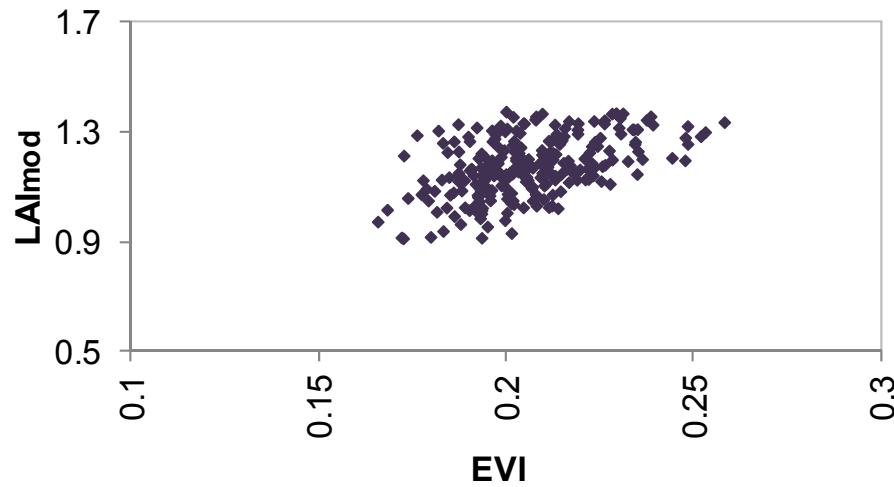
Parameter	Description	Value	Sources*
$\text{LAI}_{\text{max}}$	Maximum LAI [ $\text{m}^2 \text{ leaf m}^{-2}$ vegetation]	1.4	calib.
$k_l$	Leaf natural decay factor [ $\text{d}^{-1}$ ]	0.00137	1, 2
SLA	Specific leaf area [ $\text{m}^2 \text{ leaf kg}^{-1}$ DM]	1.6	calib.
$I_{\text{max}}$	Maximum interception [ $\text{mm d}^{-1}$ ]	1	calib.
$\theta_{\text{lim}}, \theta_{\text{cr}}$	Limit (lim), critical (cr) soil moisture [ $\text{m}^3 \text{ H}_2\text{O m}^{-3}$ soil]	0.109, 0.256	calc.(3)
$r_1$	Fraction of roots in upper soil layer [-]	0.1	calib.
$d_1, d_2$	Thickness of soil layers [mm]	50, 950	calib.
$\Psi_{\text{ae}}$	Air entry matric potential for loam [MPa]	1.43E-03	3
$\Psi_{\text{lim}}, \Psi_{\text{cr}}$	Matric potential at limit (lim), critical (cr) points [MPa]	3, 0.03	4
$n$	Porosity [ $\text{m}^3 \text{ void m}^{-3}$ soil]	0.451	3
$b$	Soil parameter for loam [-]	5.39	3
$\omega$	Conversion of $\text{CO}_2$ to DM [ $\text{kg DM kg}^{-1} \text{ CO}_2$ ]	0.54	calib.
LUE	Light use efficiency [ $\text{kg C m}^{-2} \text{ MJ}^{-1}$ ]	2.1	calib.
$f_t$	Vegetation fractional cover	0.89	calib.

\*: 1. Ceballos and Ruiz de la Torre (1979); 2. Calatayud et al.(2000); 3. Clapp and Hornberger (1978); 4. Laio et al. (2001).



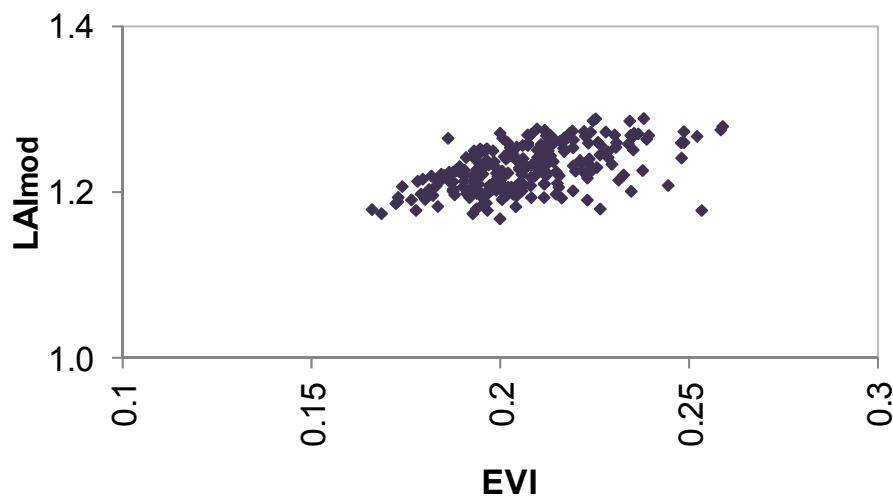
WUE-model  
 $r = 0.45$





WUE-model

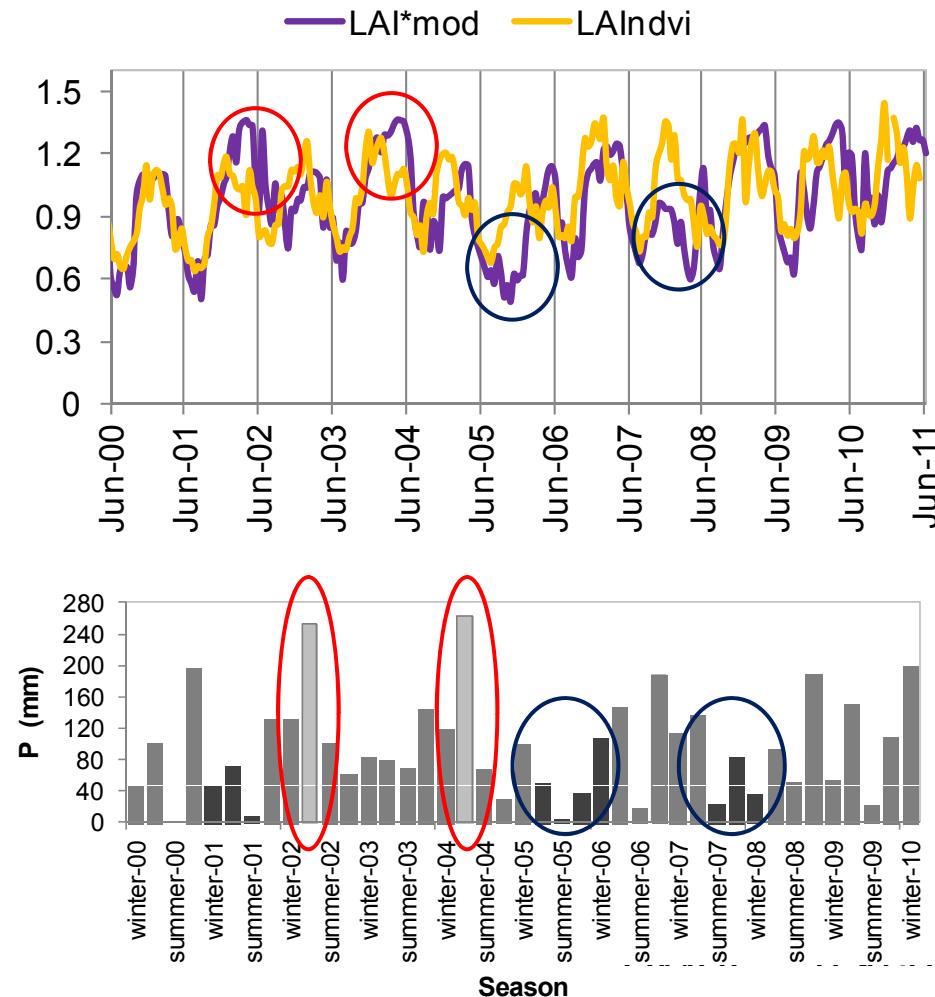
$r = 0.45$



LUE-model  
 $r = 0.57$



## LAI\*<sub>mod</sub> vs. LAI<sub>ndvi</sub>



WUE-model

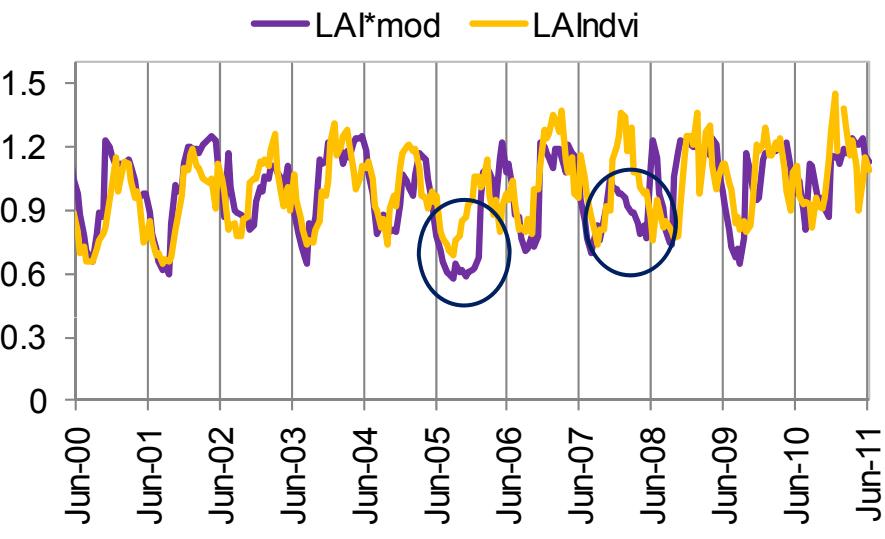
$r = 0.61$

RMSE = 0.181

LUE-model

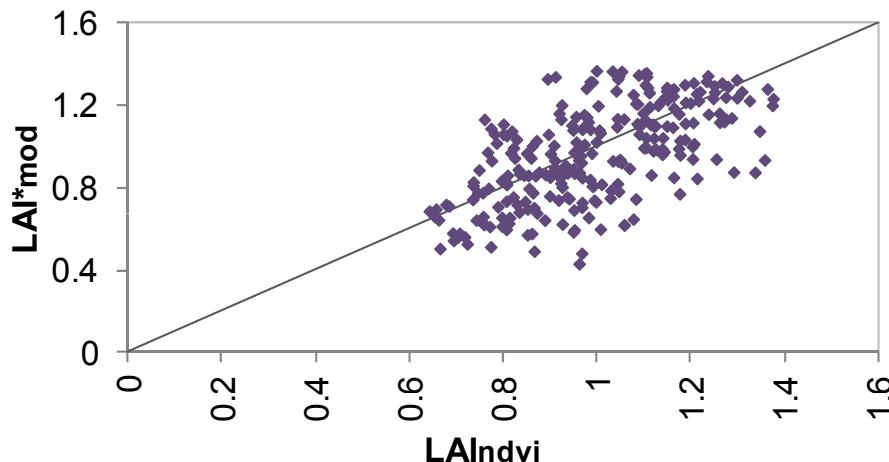
$r = 0.60$

RMSE = 0.162





## LAI<sup>\*</sup><sub>mod</sub> vs. LAI<sub>ndvi</sub>

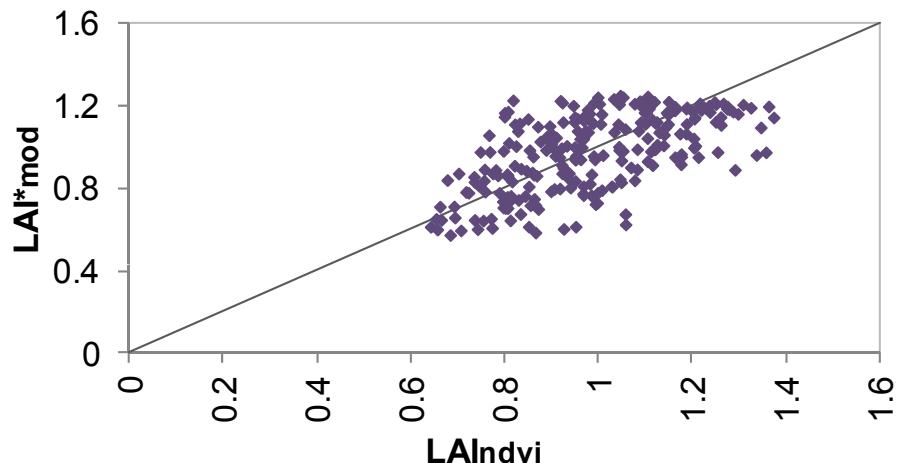


WUE-model

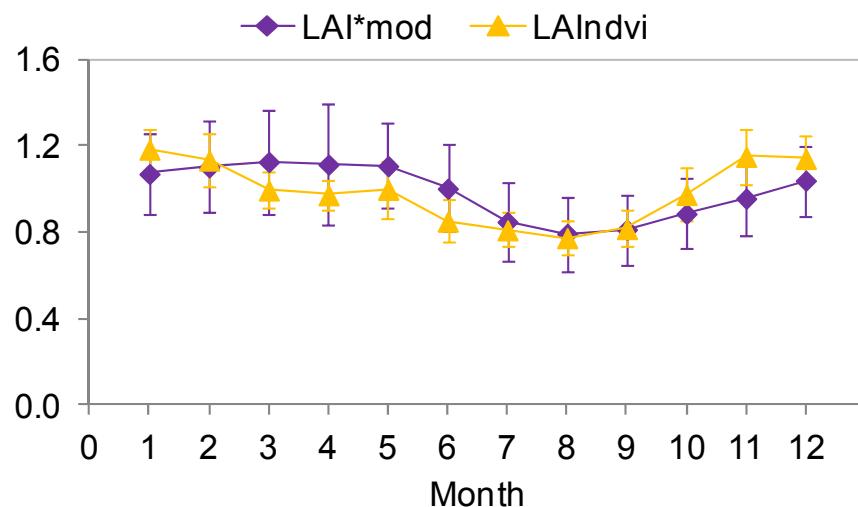
$r = 0.45$

RMSE = 0.181

LUE-model  
 $r = 0.57$   
RMSE = 0.162



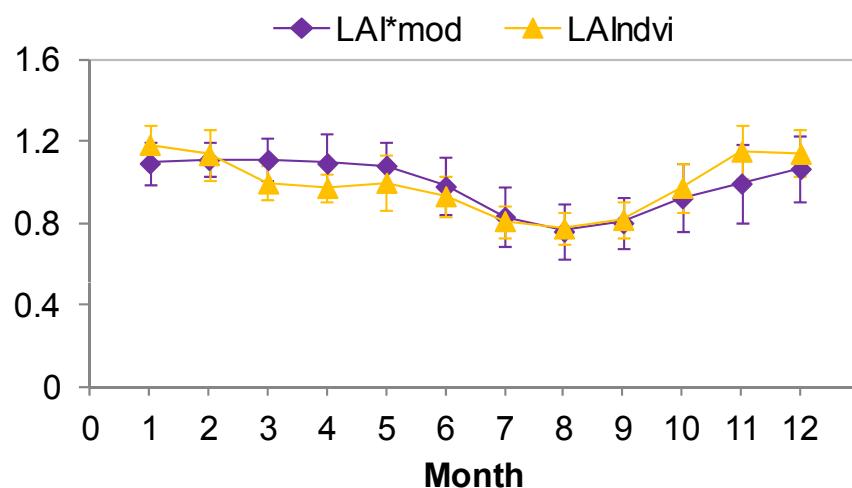
# LAI\*<sub>mod</sub> vs. LAI<sub>ndvi</sub>



WUE-model

r = 0.65

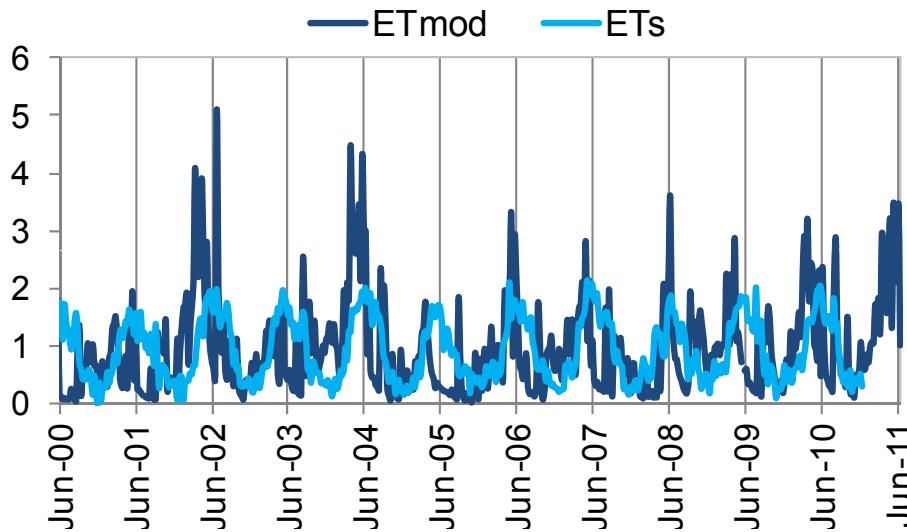
RMSE = 0.11



LUE-model

r = 0.85

RMSE = 0.07



WUE-model

r = 0.28

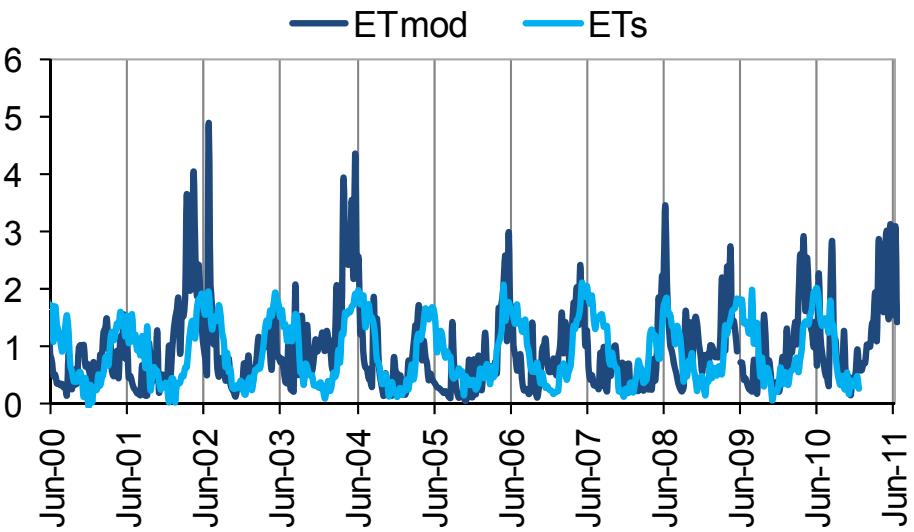
RMSE = 0.82

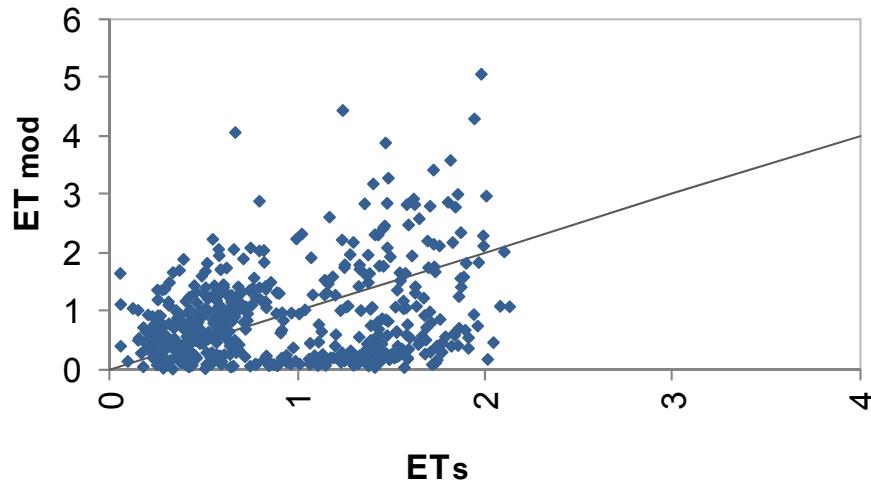
ET decline in  
July-August?

LUE-model

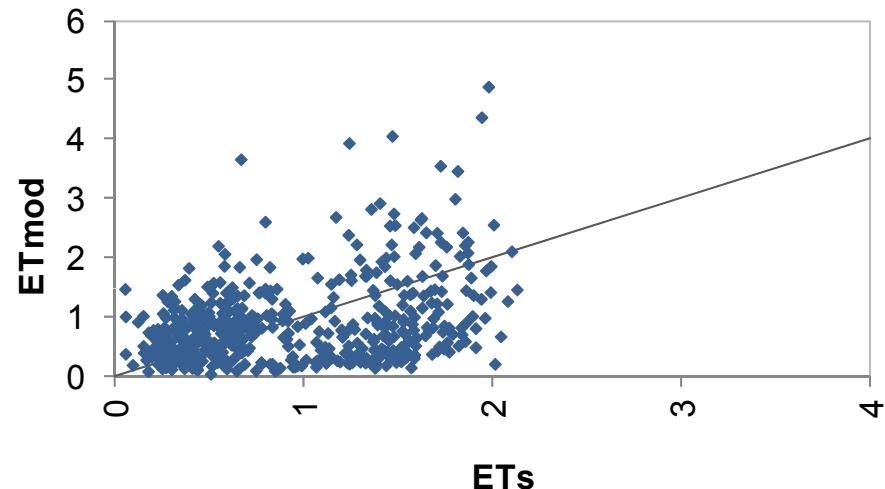
r = 0.35

RMSE = 0.72





LUE-model  
 $r = 0.35$



From GSA and GLUE analysis →

- 2 models, similar behaviour
- poor performance linked to drought periods

After the calibration: same qualities and problems evidenced by the sensitivity analysis (problems WUE wet springs)

LUE-model performed best: agreement with EVI and  $\text{LAI}_{\text{NDVI}}$

# Conclusions – Issues

Role of vegetation in hydrological systems → important  
Relationships soil-veg. → highly non-linear



**appropriate vegetation modelling** → crucial  
(water resources, flood risk...climate change?!)

Two basic issues:

1. Which **model** (how to choose?)
2. Careful **interpretation** of each **remote-sensing product**  
(vegetation indices supply indirect information)

# Conclusions – Satellite data

**EVI**: well correlated with leaf biomass

**NDVI**: dependence on soil moisture

**LAI**: wrong classification veg. cover

**ET**: correlated with ETo, algorithm depends on LAI



**BE  
CAREFUL**

## VEGETATION MODELS:

- HORAS → failed to reproduce annual cycle
- WUE-model → specific for water limited climates  
(control on growth through T)
- LUE-model → widely applicable (change  $\varepsilon$  formulation)  
best results

Recommended  
LUE-model

## Future research lines

- Implement the models at a **distributed level** and couple them with a distributed hydrological model
- Use of **satellite soil moisture** estimation (e.g. SMOS, ASCAT)
- Consider **other** environmental **stresses** in addition to water stress (temperature, nutrients)
- **Competition and succession** conceptualization (herbaceous vegetation and open canopy)

## Paper - will be submitted shortly:

Pasquato M, Medici C, Friend AD, Francés F. Comparing two approaches for parsimonious vegetation modelling in semiarid regions using satellite data. *Ecohydrology*

## Participations in congresses:

Pasquato M, Medici C, Francés F. 2013. Assessing a parsimonious eco-hydrological model implementation to an Aleppo pine semiarid forest through available remote sensing data. *AGU Fall Meeting*. San Francisco, USA. ([poster](#))

Pasquato M, Medici C, Friend AD, Francés F. 2013. Comparing modelled and remotely sensed leaf area dynamics in an Aleppo pine semiarid forest. *EGU General assembly*. Vienna, Austria. ([poster](#))

Pasquato M, Medici C, Francés F. 2011. Aplicación de un modelo conceptual distribuido de vegetación dinámica a una cuenca semiárida del SE de España. *Symposium on Vadose Zone*. Salamanca, Spain. ([poster and article in Book of Proceedings](#))

Pasquato M, Medici C, Francés F. 2011. Application of a conceptual distributed dynamic vegetation model to a semi-arid basin, SE of Spain. *EGU General assembly*. Vienna, Austria. ([oral presentation](#))

Francés F, Medici C, Bussi G, García A, Barrios M, Pasquato M. 2010. Distributed hydrological modelling within SCARCE Project: integrating water, sediment, quality and vegetation. *SCARCE Annual Conference*. Girona, Spain. ([oral presentation and article in Book of Proceedings](#))

**THANK YOU  
FOR YOUR ATTENTION**



**UNIVERSITAT  
POLITECNICA  
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**Instituto de Ingeniería del  
Agua y Medio Ambiente**

**Programa de Doctorado de  
Ingeniería Hidráulica y  
Medio Ambiente**



Grupo de Investigación de Modelación Hidrológica y Ambiental



$$\frac{dH}{dt} = (P - I) - L - E - T$$

WATER BALANCE EQ.

$$I = \min(P \cdot R, I_{\max} \cdot R - J)$$

INTERCEPTION

$$\frac{dJ}{dt} = I - \min(ET_o \cdot R, J)$$

INTERCEPTION STORAGE

$$T = \min(ET_o \cdot R \cdot \beta_t, ET_o - E_i, H)$$

TRANSPIRATION

$$E = \min \left[ H \cdot \left( \frac{z_{ss}}{z_e} \right) \cdot (1 - R), ET_o - E_i - T \right]$$

BARE SOIL  
EVAPORATION

$$\left. \begin{array}{l} \frac{dH_1}{dt} = (P - I) - D - E - T_1 \\ \frac{dH_2}{dt} = D - L - T_2 \end{array} \right\}$$

WATER BALANCE EQ.

$$I = \min(P \cdot f_t, I_{\max} \cdot f_t - J)$$

INTERCEPTION

$$\frac{dJ}{dt} = I - \min(ET_o \cdot f_t, J)$$

INTERCEPTION STORAGE

$$T_1 = [ET_o \cdot f_t - \min(ET_o \cdot f_t, J)] \cdot \min(LAI_{\text{mod}}, 1) \cdot \beta_t(H_1) \cdot r_1$$

TRANSPIRATION

$$T_2 = [ET_o \cdot f_t - \min(ET_o \cdot f_t, J)] \cdot \min(LAI_{\text{mod}}, 1) \cdot \beta_t(H_2) \cdot (1 - r_1)$$

$$E = ET_o \cdot f_b \cdot \beta_b(H_1)$$

BARE SOIL  
EVAPORATION

# WUE-/LUE- MODEL

$$Re = r \cdot \frac{C}{cn} \cdot \phi \cdot g(Temp)$$

MAINTENANCE RESPIRATION

$$\varphi = 1 - \frac{LAI}{LAI_{\max}}$$

ALLOCATION FACTOR

$$LAI_{\text{mod}} = B_l \cdot SLA \cdot f_t$$

GROUND BASED LAI

$$LAI^{*}_{\text{mod}} = LAI_{\text{mod}} \cdot \left(1 - \bar{\zeta}_{10}\right)$$

CORRECTED LAI

$$\zeta_{tot} = \zeta(H_1) \cdot r_1 + \zeta(H_2) \cdot (1 - r_1)$$

TOTAL WATER STRESS