



Importance of the spatial heterogeneity in the non-linear response of a small Mediterranean catchment

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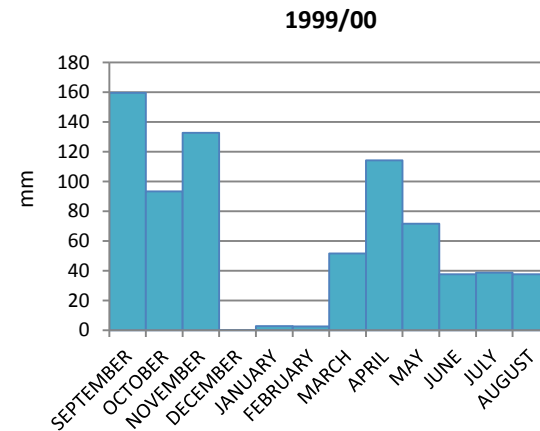
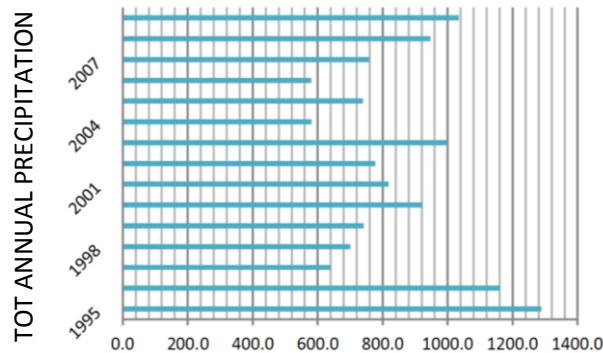
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INTRODUCTION

- ❑ Mediterranean basins
- ❑ Non-linear hydrological behaviour

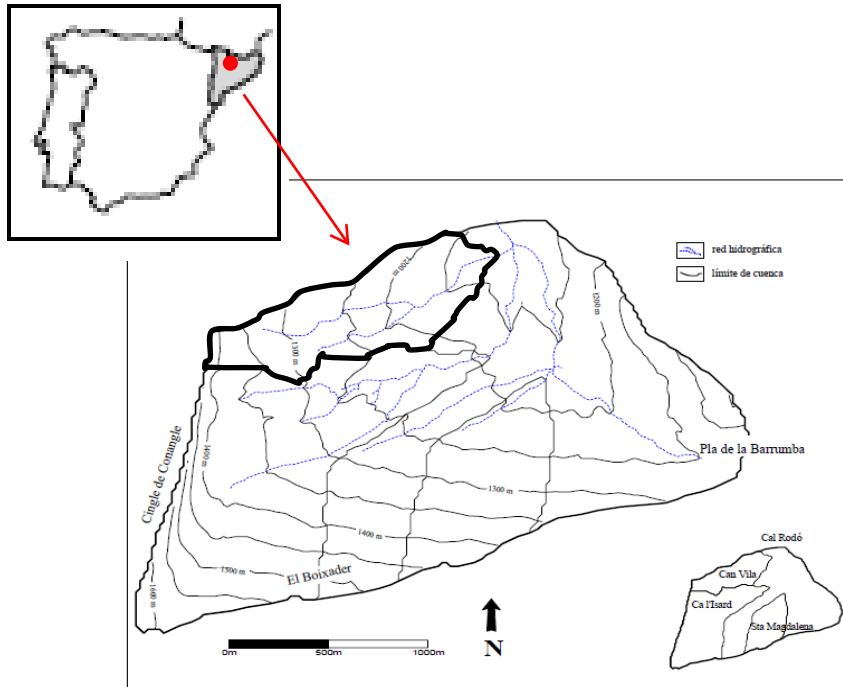


Large inter- and intra-annual precipitation variability



STUDY AREA

☐ *Can Vila* catchment:



- ✓ Experimental catchment
- ✓ Area: 0.56 km²
- ✓ Silt-loam soil
- ✓ Soil thickness: 0.15-3.0 m



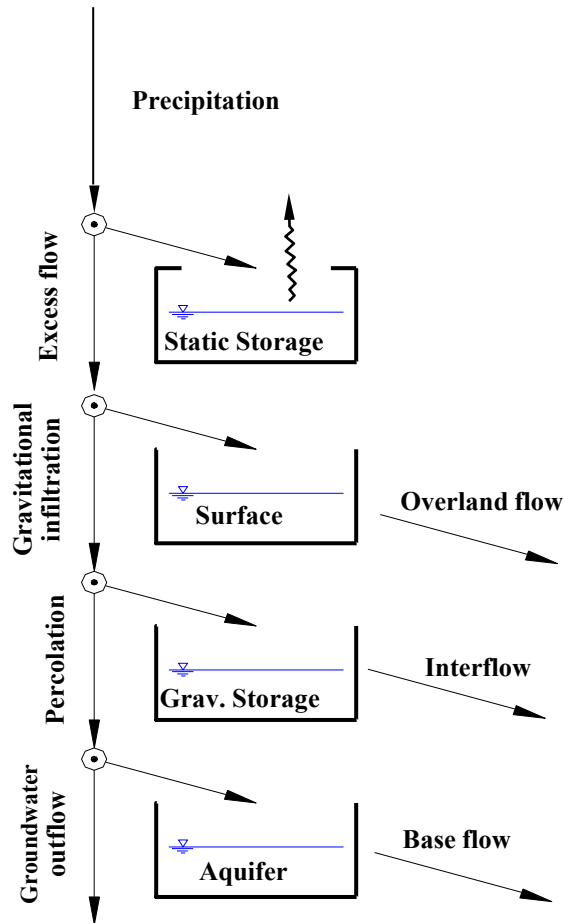
INTRODUCTION

□ *Research questions:*

1. Can we reproduce its hydrological behaviour with a *simple lumped model* based on few parameters?
2. If not, it is because a *non-linear mechanism is missing* into the model conceptual scheme or it is because we are not taking into account the *catchment spatial heterogeneity*?
3. Which is the most suitable approach, *lumped or distributed*, to simulate the discharge at the outlet of the study case considered?



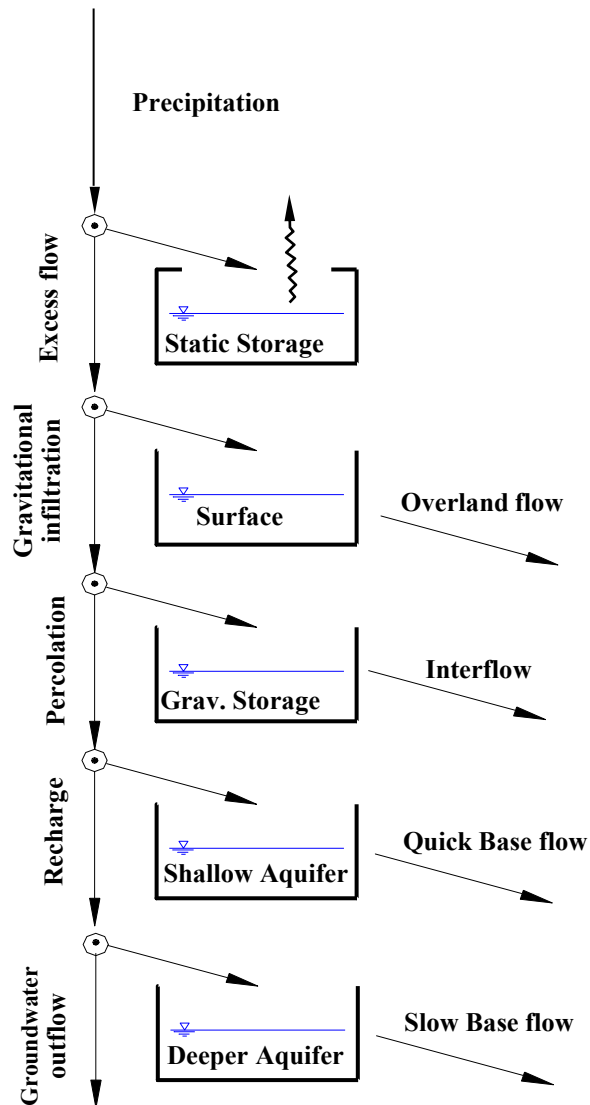
HYDROLOGICAL MODELS



- ✓ **LU3 – LUMPED MODEL**
- ✓ **6 parameters** to be calibrated
- ✓ 3 catchment hydrological responses
- ✓ Linear tanks



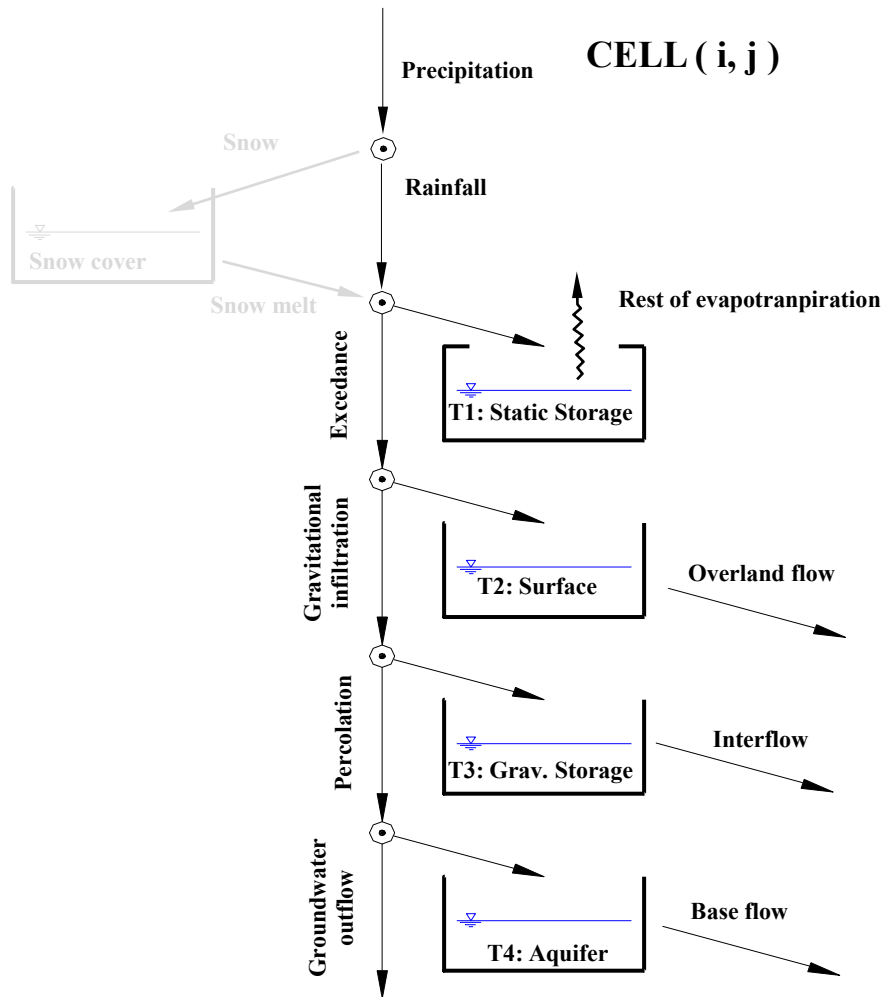
HYDROLOGICAL MODELS



- ✓ **LU4 – LUMPED MODEL**
- ✓ **8 parameters** to be calibrated
- ✓ 4 catchment hydrological responses
- ✓ Linear tanks
- ✓ **Non-linear recharge** to the permanent saturated zone



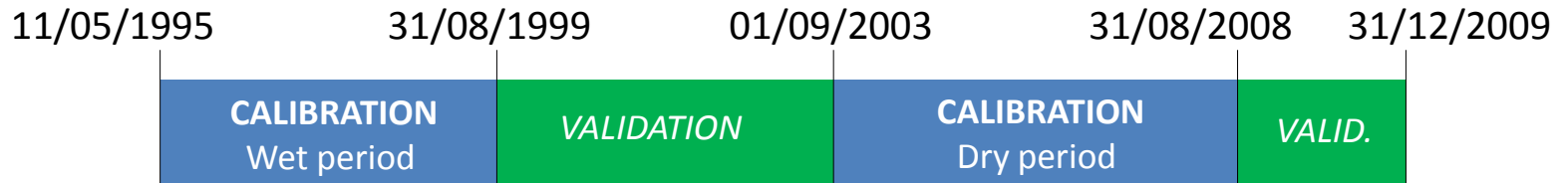
HYDROLOGICAL MODELS



- ✓ **TETIS – DISTRIBUTED CONCEPTUAL MODEL**
- ✓ **8 correction factors** to be calibrated
- ✓ Several soil-related parameter maps to be estimated
- ✓ 3 catchment hydrological responses
- ✓ Linear tanks



CALIBRATION & VALIDATION



***Nash-Sutcliffe efficiency
index***

$$E = 1 - \frac{\sum_1^n (X_{sim} - X_{obs})^2}{\sum_1^n (X_{obs} - \bar{X}_{obs})^2}$$

Volume error

$$V = \frac{\sum_1^n (X_{sim} - X_{obs})}{\sum_1^n X_{obs}}$$

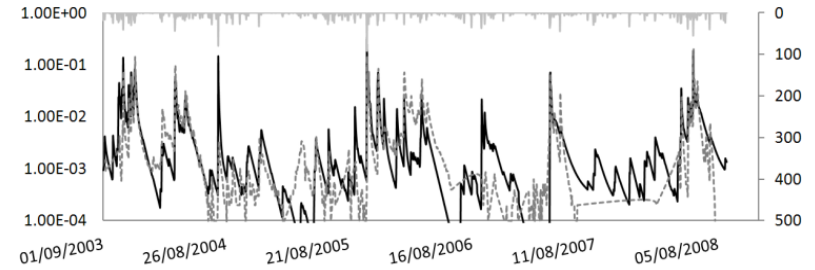
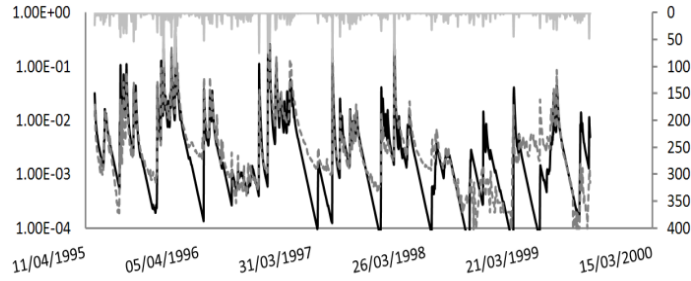


CALIBRATION RESULTS:

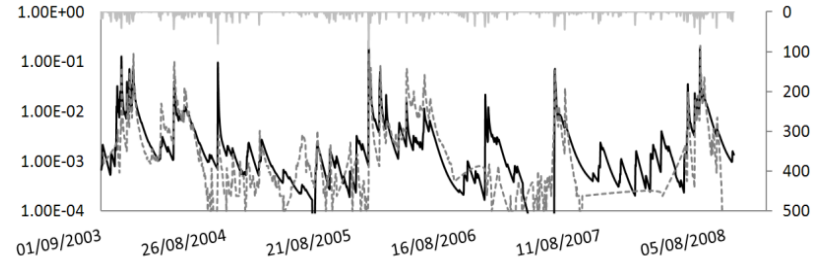
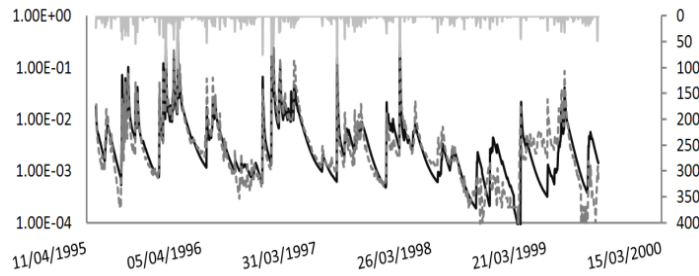
WET PERIOD

DRY PERIOD

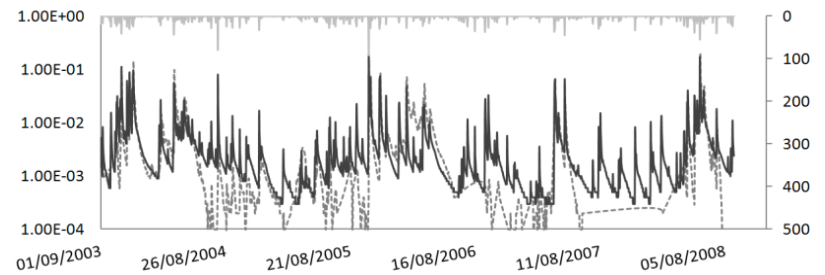
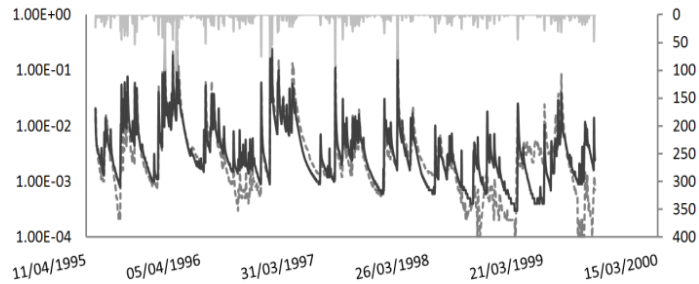
LU3



LU4



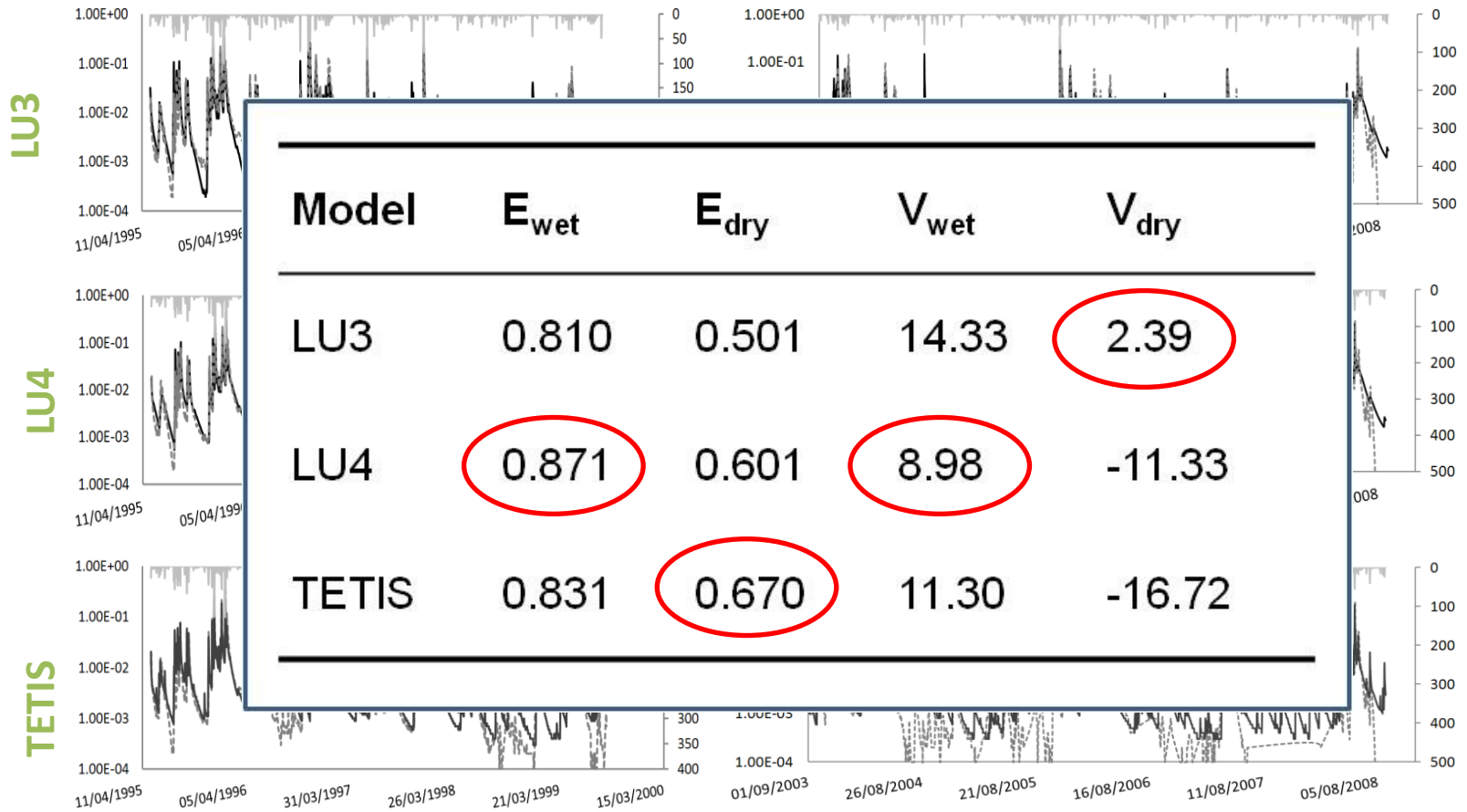
TETIS



CALIBRATION RESULTS:

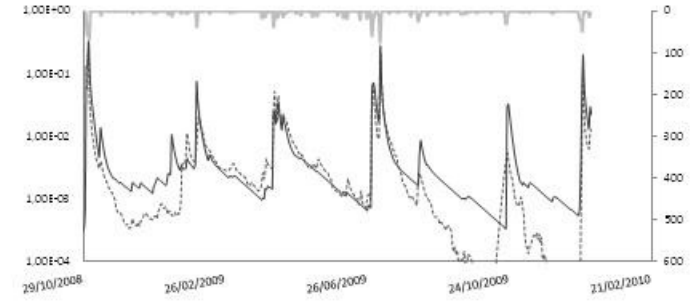
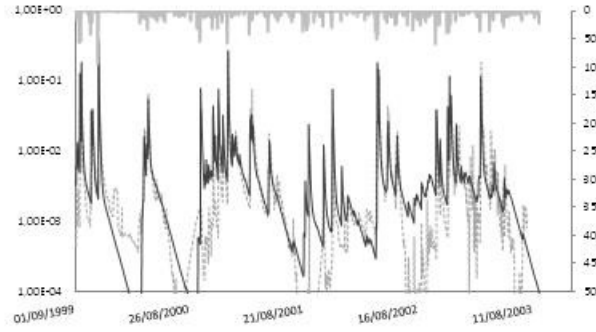
WET PERIOD

DRY PERIOD

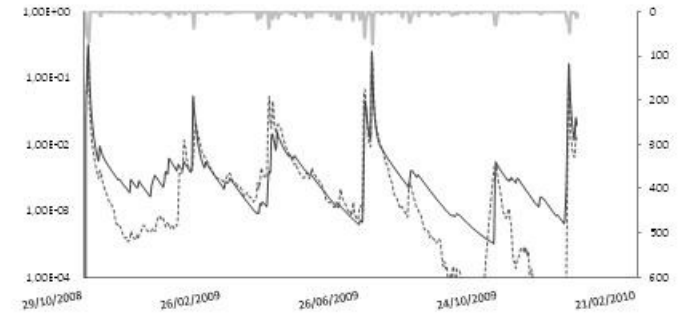
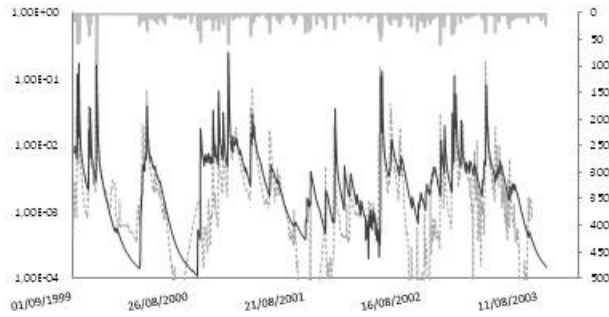


VALIDATION RESULTS

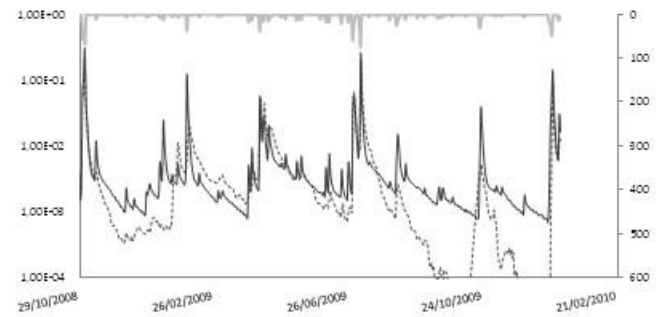
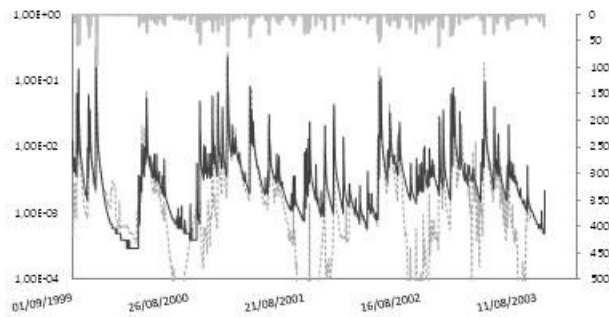
LU3



LU4

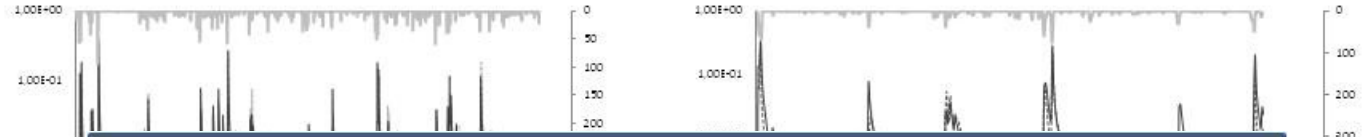


TETIS

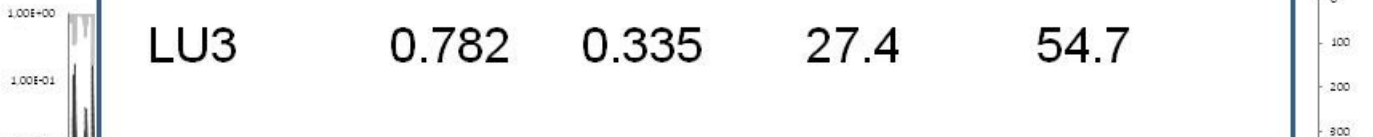


VALIDATION RESULTS

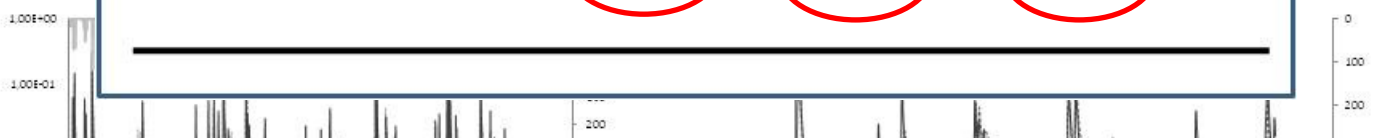
LU3



LU4



TETIS



| Model | E_1 | E_2 | V_1 | V_2 |
|-------|-------|-------|-------|-------|
| LU3 | 0.782 | 0.335 | 27.4 | 54.7 |
| LU4 | 0.826 | 0.537 | 21.7 | 35.3 |
| TETIS | 0.812 | 0.623 | 21.5 | 32.4 |

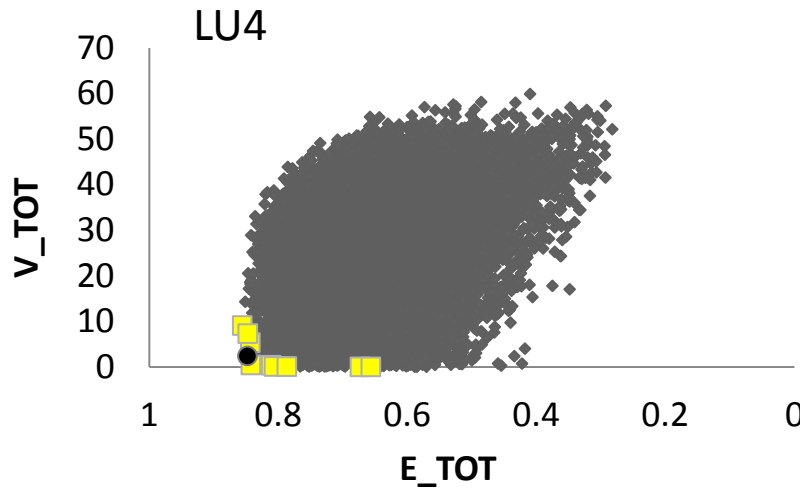


PARETO FRONTIER ANALYSIS

- ✓ 10.000 Monte Carlo (MC) simulations
- ✓ Parameters values were sampled randomly by UNIFORM distributions



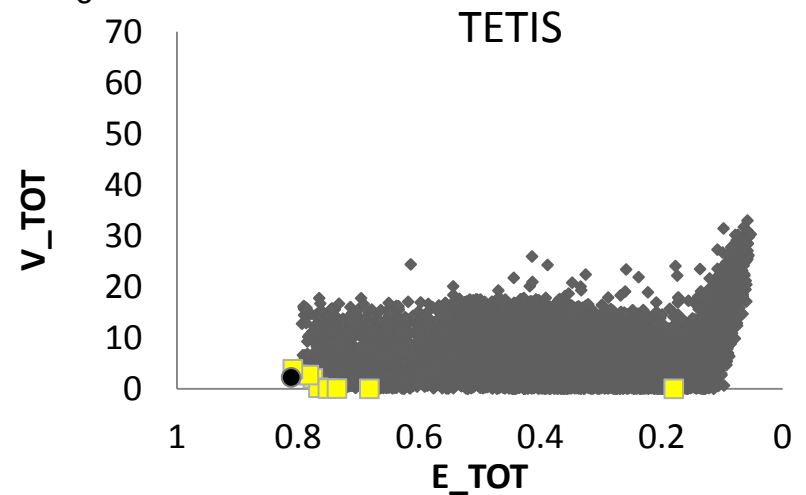
PARETO FRONTIER



- ◆ MC simulations
- Pareto frontier
- Optimum parameter set

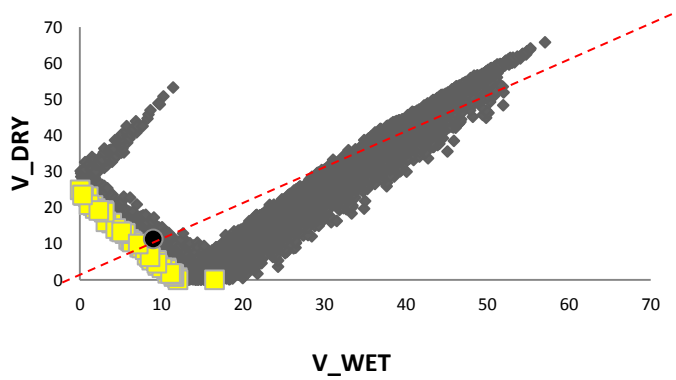
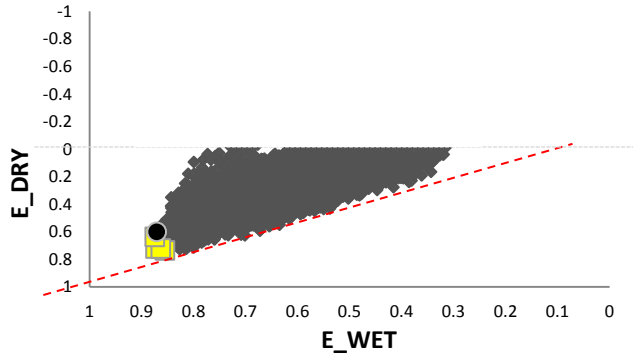
E_{TOT} : Nash index

V_{TOT} : Volume Error



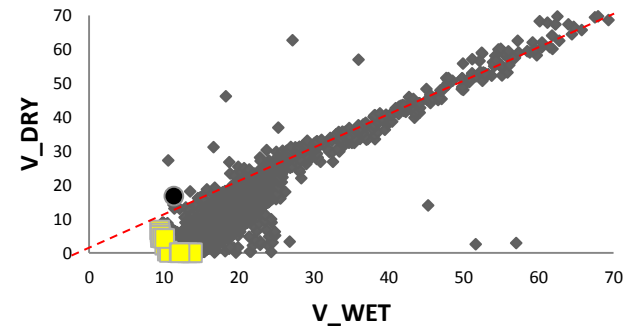
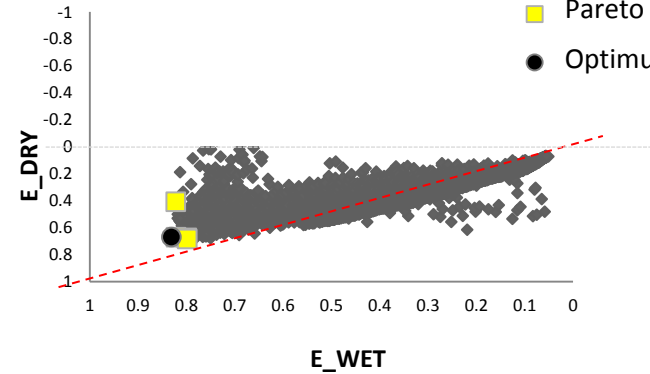
PARETO FRONTIER

LU4 model

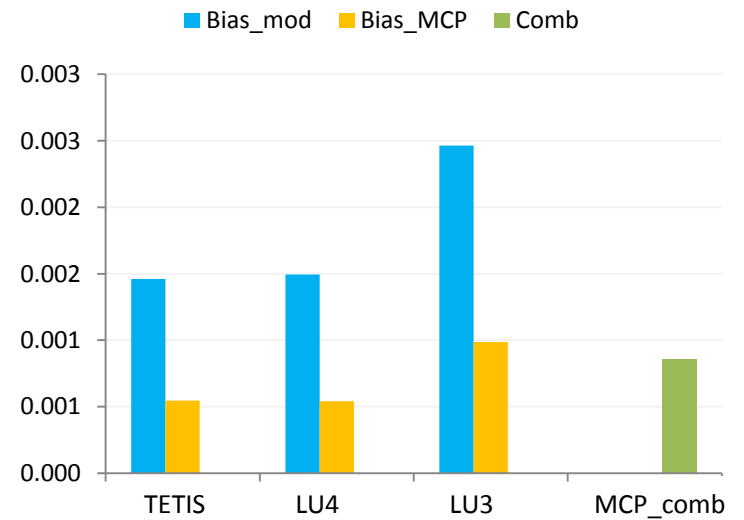
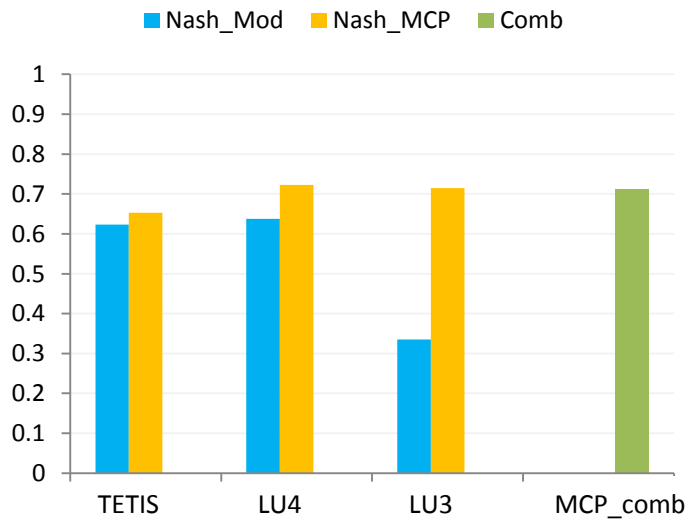
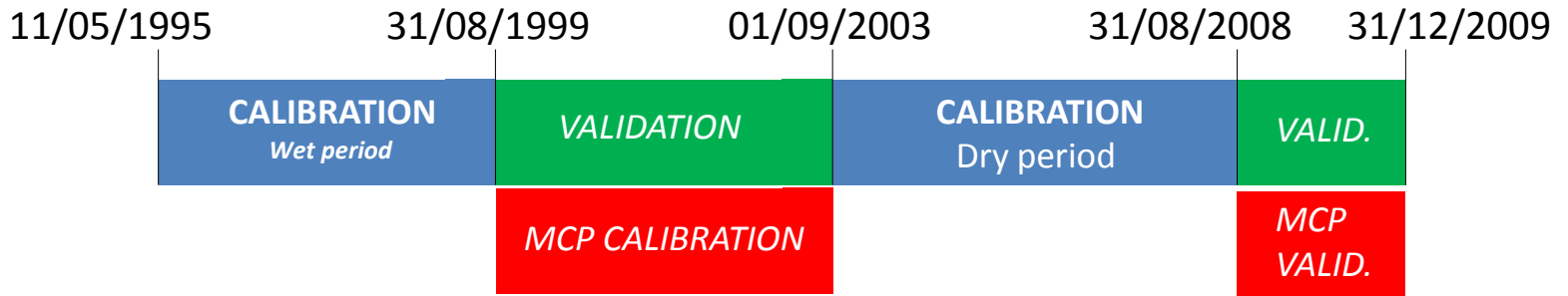


TETIS model

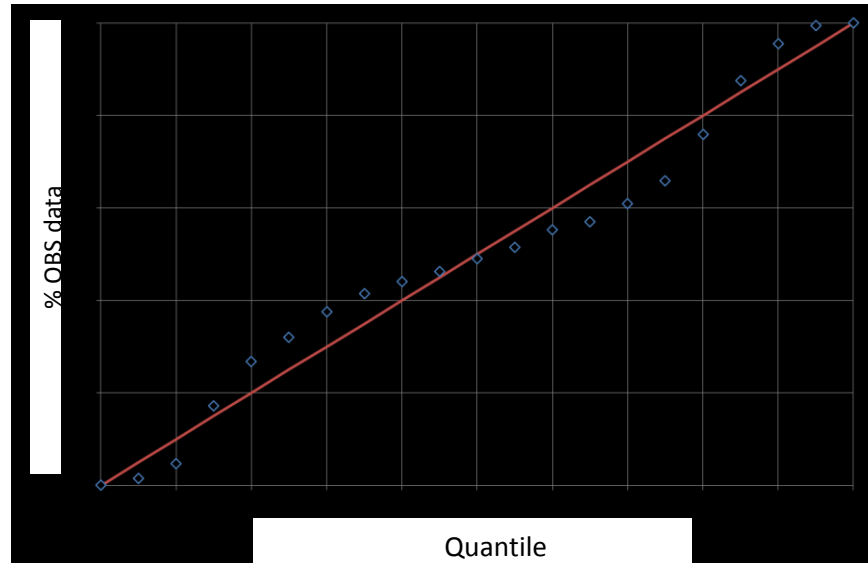
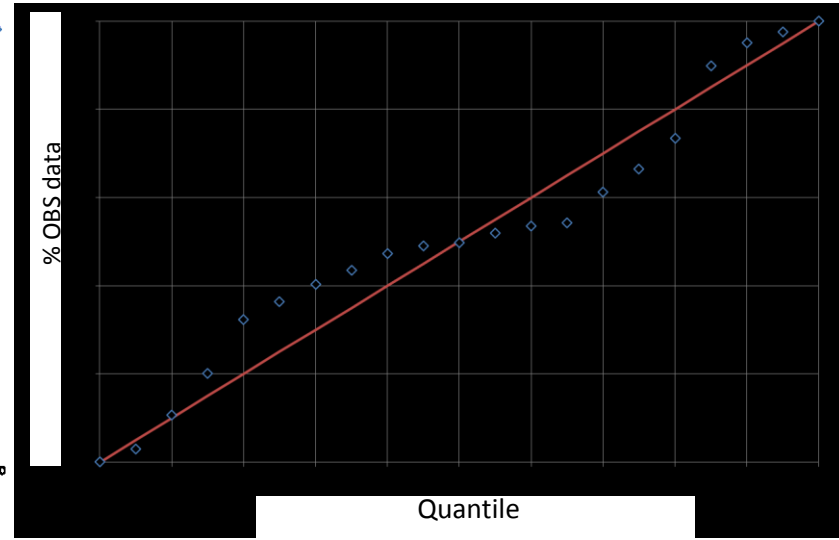
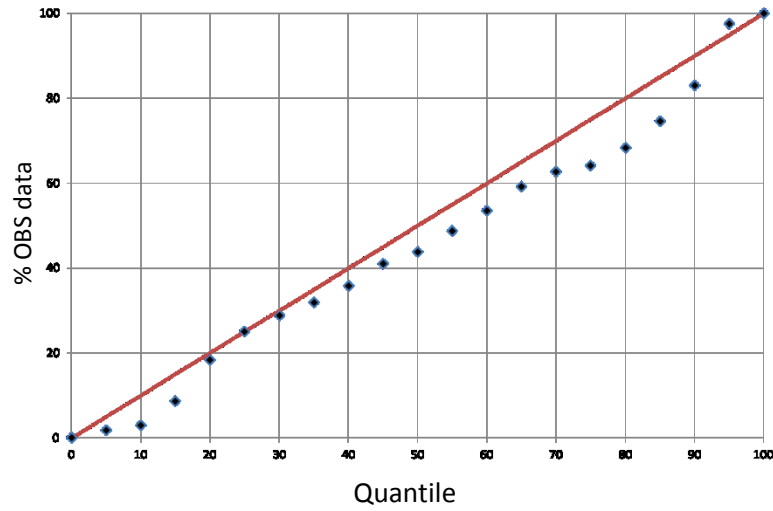
- ◆ MC simulations
- Pareto frontier
- Optimum set



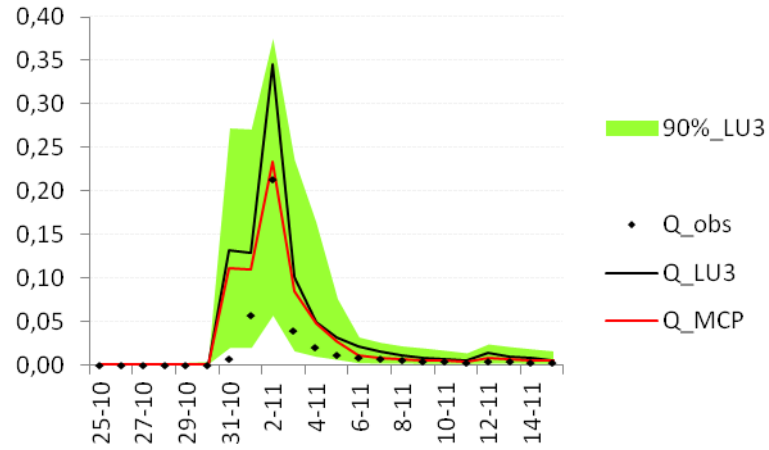
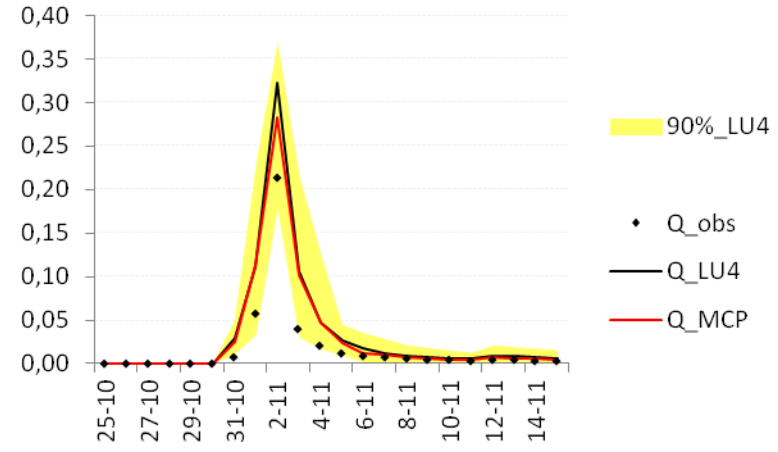
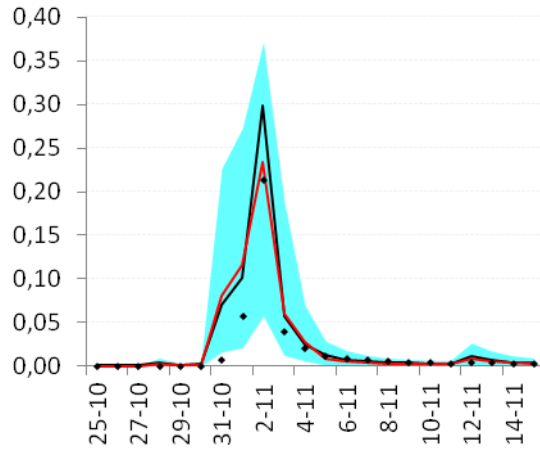
MCP ANALYSIS



MCP ANALYSIS - RELIABILITY



MCP ANALYSIS



MCP ANALYSIS

UNCERTAINTY ANALYSIS

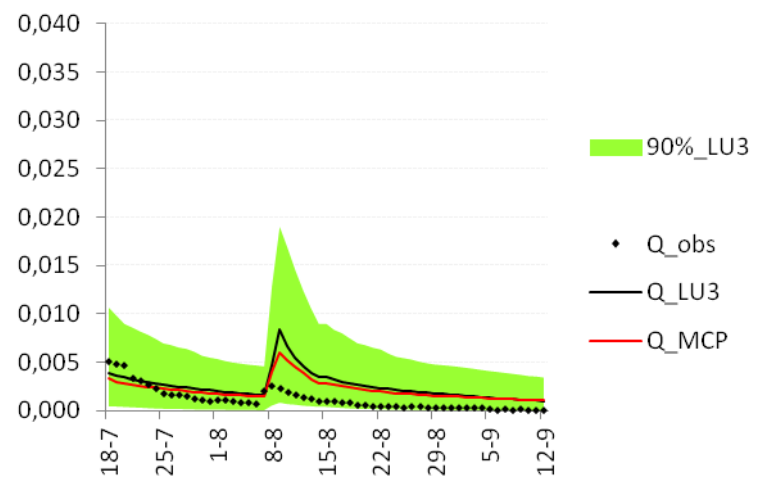
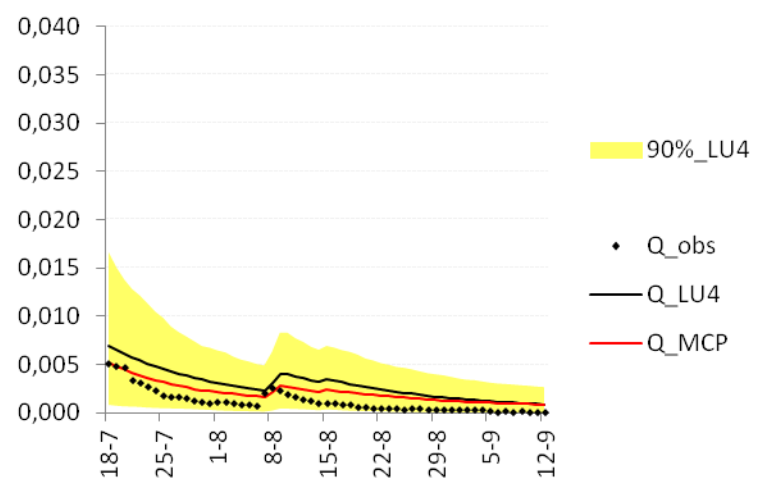
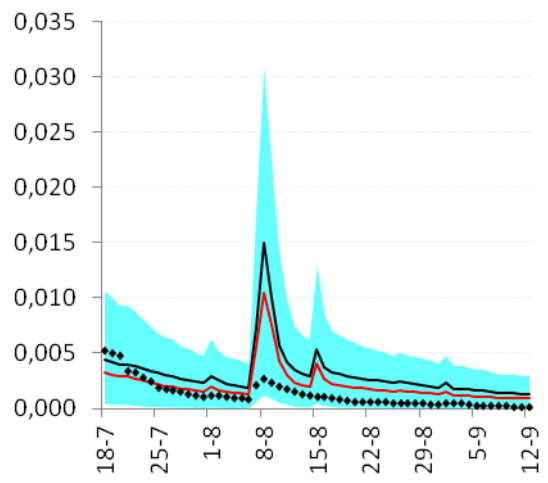
MULTI-OBJECTIVE ANALYSIS

CALIBRATION AND VALIDATION

HYDROLOGICAL MODELS

STUDY AREA

INTRODUCTION



MCP ANALYSIS – Band's width

| | Tot | Recessions | Events | Recession limbs band's increment | Events band's increment |
|----------------------|--------|------------|--------|----------------------------------|-------------------------|
| TETIS | 0,0086 | 0,0062 | 0,1365 | 0,0% | 46,1% |
| LU4 | 0,0074 | 0,0070 | 0,0935 | 12,9% | 0,0% |
| LU3 | 0,0094 | 0,0081 | 0,1561 | 31,1% | 67,0% |
| MCP_TETIS_LU3 | 0,0130 | 0,0073 | 0,1361 | 3,8% | 25,0% |
| MCP_TETIS_LU4 | 0,0110 | 0,0070 | 0,1134 | 0,0% | 4,1% |
| MCP_LU3_LU4 | 0,0120 | 0,0075 | 0,1088 | 6,9% | 0,0% |



CONCLUSIONS

- ✓ The **deterministic approach** pointed out:
 - The simplest lumped model **LU3** provided the worst results
 - The non-linear lumped model **LU4** performed slightly better than the distributed **TETIS** model for the wet period, while the latter gave better results during the dry periods
- ✓ The **Pareto frontier** analysis pointed out:
 - The calibrated optimum parameter sets were included into the Pareto frontier
 - The TETIS model showed a more consistent behaviour in terms of the dispersion of the cloud of points
- ✓ The **MCP analysis** pointed out
 - The LU4 provided the narrowest band for the discharge events
 - The TETIS model provided the narrowest band for the recession limbs
 - A MCP combination of the LU4 and TETIS gave the best result in terms of predictive uncertainty



CONCLUSIONS

- ✓ We could not simulate the non linear discharge behaviour at the outlet of this small Mediterranean catchment with the simplest lumped model LU3
- ✓ The non-linear mechanism seems to be relevant during the high discharge period
- ✓ The spatial heterogeneity may have a key role during the driest periods
- ✓ A combination of the two approaches may represent the solution to guarantee the most reliable results
- ✓ The inclusion of a non-linear percolation mechanism will be tested in the future

